

Introduction to OpenMP

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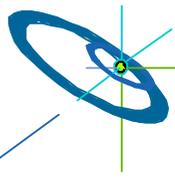


Outline

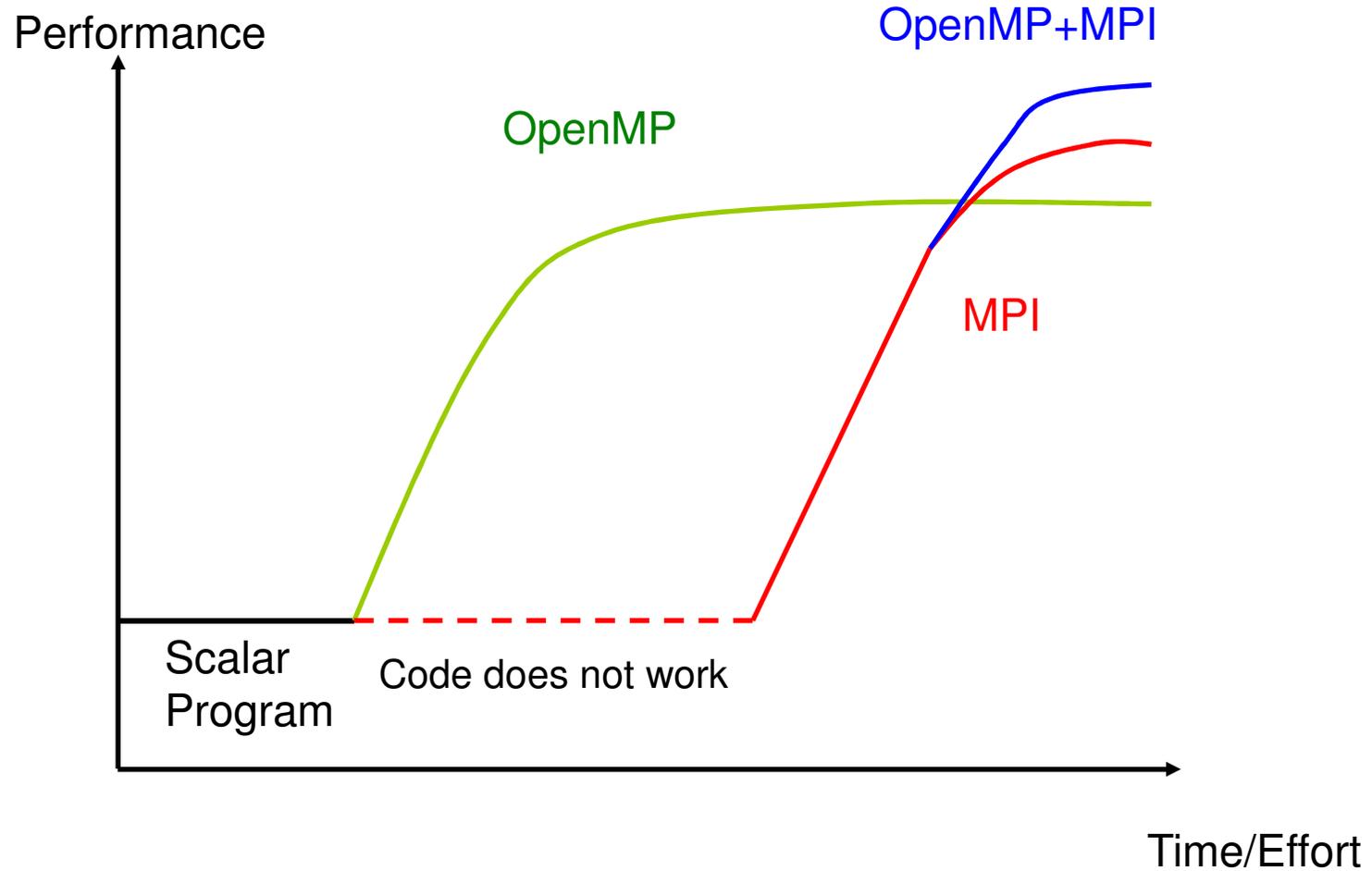
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OpenMP Overview: What is OpenMP?

- OpenMP is a standard programming model for shared memory parallel programming
- Portable across all shared-memory architectures
- It allows incremental parallelization
- Compiler based extensions to existing programming languages
 - mainly by directives
 - a few library routines
- Fortran and C/C++ binding
- OpenMP is a standard



Motivation: Why should I use OpenMP?

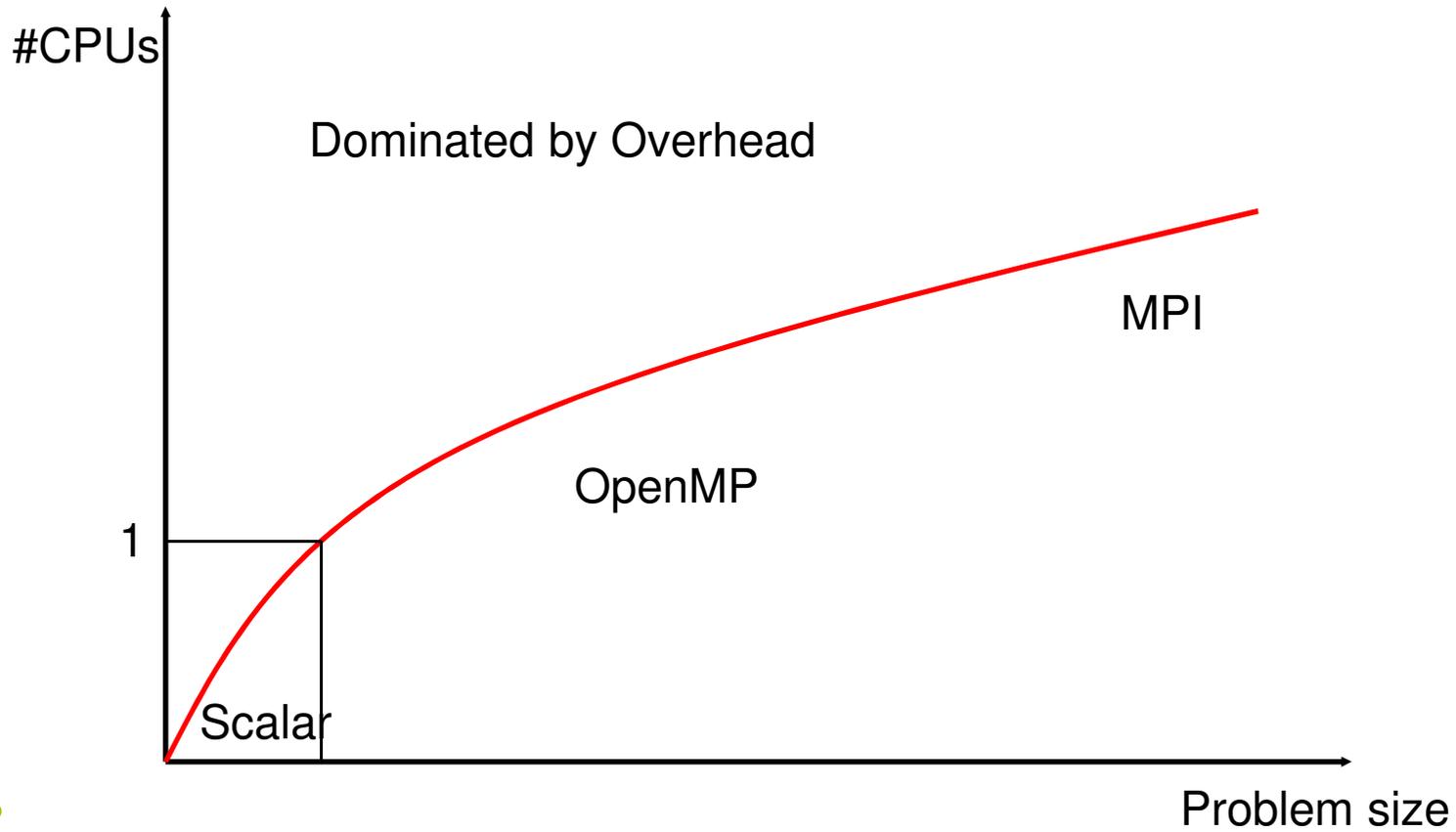


Further Motivation to use OpenMP

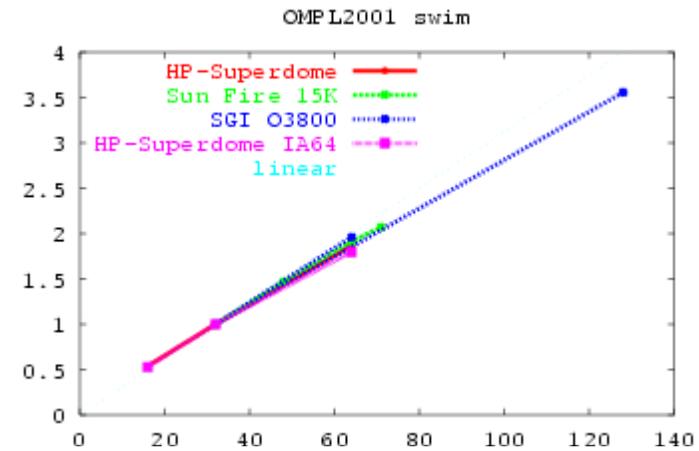
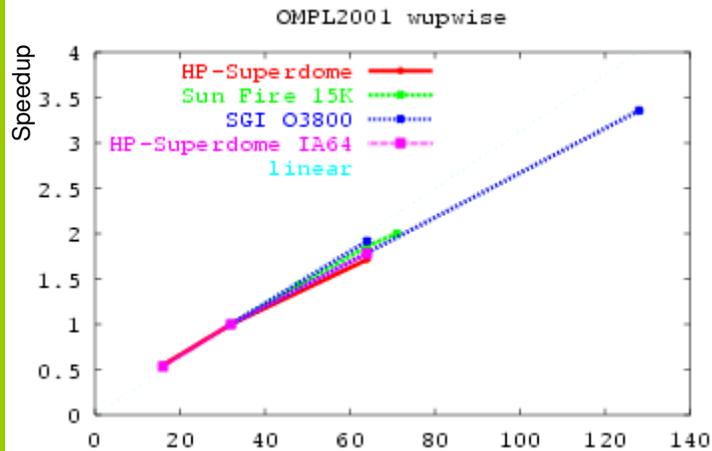
- OpenMP is the easiest approach to multi-threaded programming
- Multi-threading is needed to exploit modern hardware platforms:
 - Intel CPUs support Hyperthreading
 - AMD Opterons are building blocks for cheap SMP machines
 - A growing number of CPUs are multi-core CPUs
 - **IBM Power CPU**
 - **SUN UltraSPARC IV**
 - **HP PA8800**



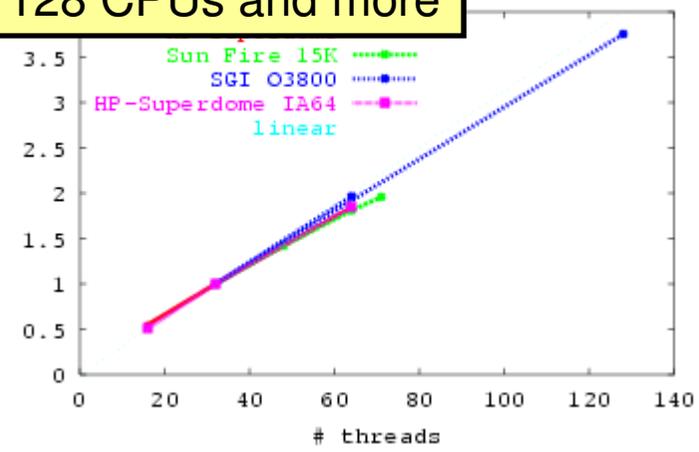
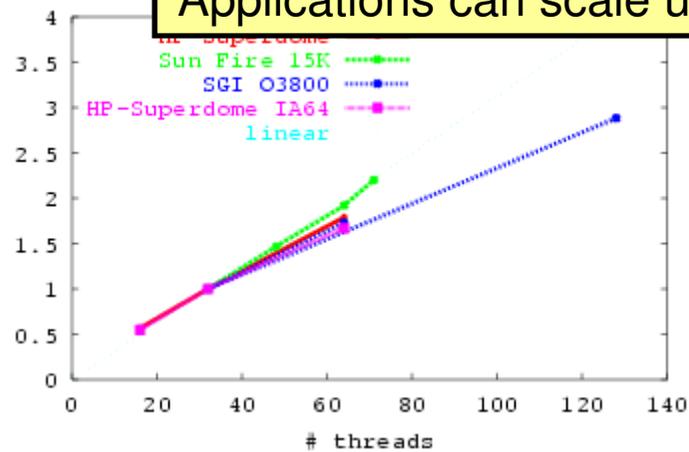
Where should I use OpenMP?



On how many CPUs can I use OpenMP?

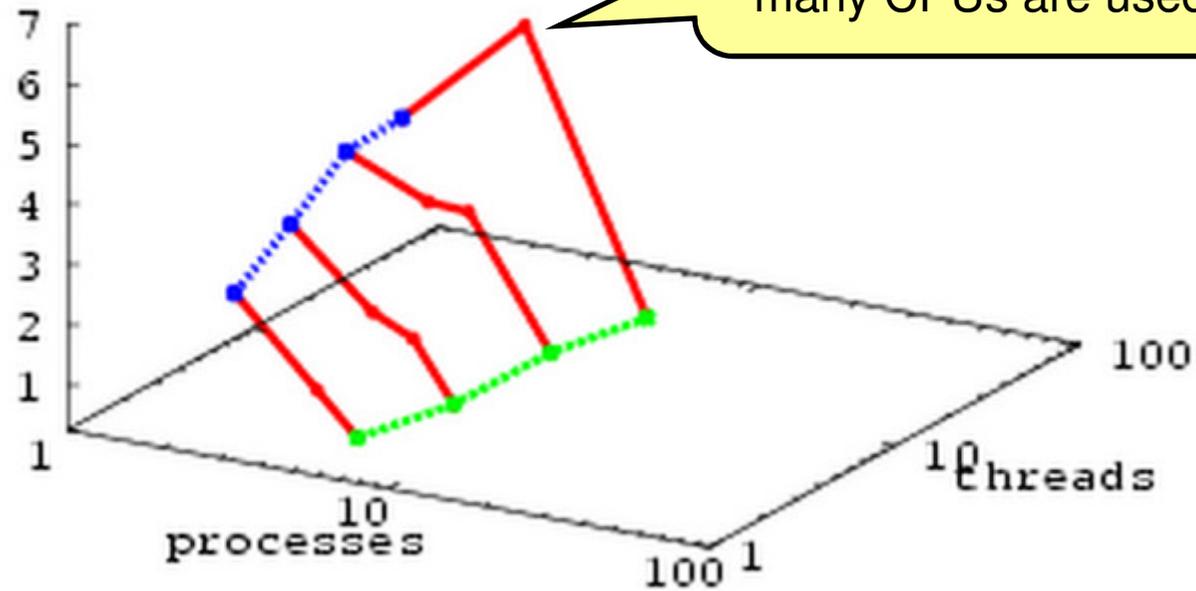


Applications can scale up to 128 CPUs and more



Hybrid Execution (OpenMP+MPI) can improve the performance

hybrid —●—
MPI●.....
OpenMP●.....



Simple OpenMP Program

- Most OpenMP constructs are compiler directives or pragmas
- The focus of OpenMP is to parallelize loops **with independent iterations**
- OpenMP offers an incremental approach to parallelism

Serial Program:

```
void main()
{
    double Res[1000];

    for(int i=0;i<1000;i++) {
        do_huge_comp(Res[i]);
    }
}
```

Parallel Program:

```
void main()
{
    double Res[1000];
    #pragma omp parallel for
    for(int i=0;i<1000;i++) {
        do_huge_comp(Res[i]);
    }
}
```

Who owns OpenMP? - OpenMP Architecture Review Board

Permanent Members of the ARB:

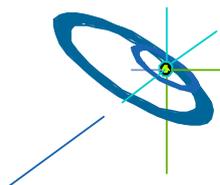
- AMD (David Leibs)
- Cray (James Beyer)
- Fujitsu (Matthijs van Waveren)
- HP (Uriel Schafer)
- IBM (Kelvin Li)
- Intel (Sanjiv Shah)
- NEC (Kazuhiro Kusano)
- The Portland Group, Inc. (Michael Wolfe)
- SGI (Lori Gilbert)
- Sun (Nawal Copty)
- Microsoft (-)

Auxiliary Members of the ARB:

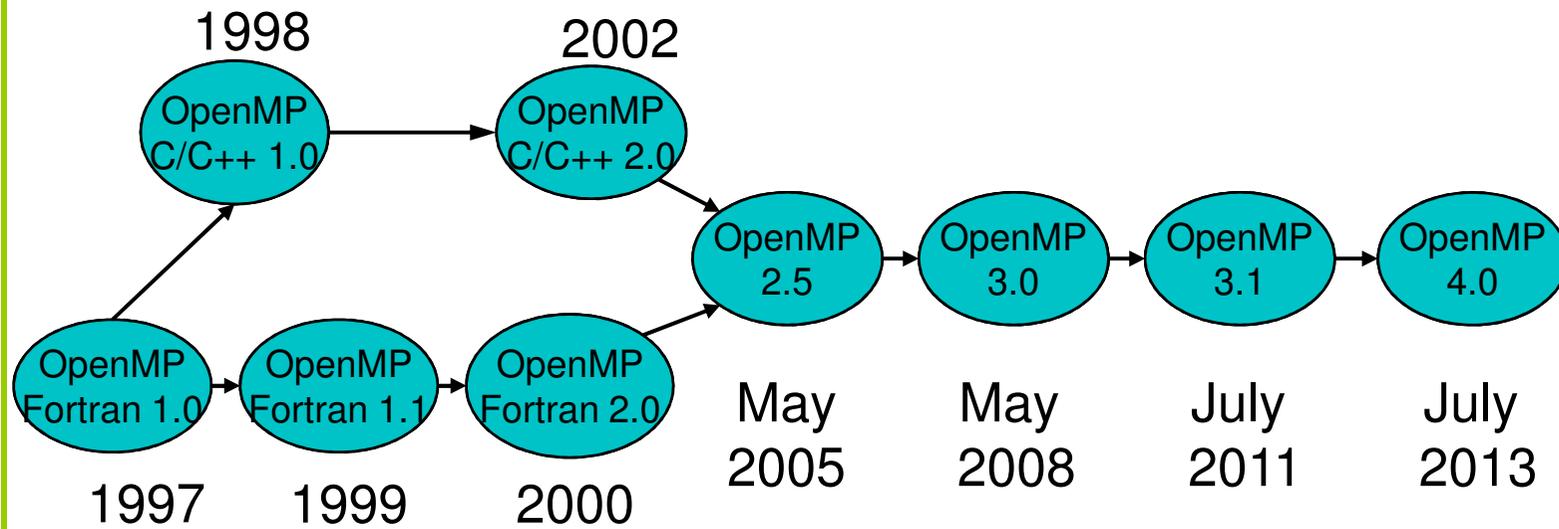
- ASC/LLNL (Bronis R. de Supinski)
- cOMPunity (Barbara Chapman)
- EPCC (Mark Bull)
- NASA (Henry Jin)
- RWTH Aachen University (Dieter an Mey)

From: <http://openmp.org/wp/about-openmp/>

Last update: May 22, 2008



OpenMP Release History



Introduction to OpenMP [07]



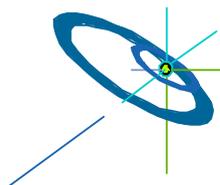
OpenMP Availability

- OpenMP 1.0 (C/C++) and OpenMP 1.1 (Fortran 90) is available on all platforms in the commercial compilers
- Most features from OpenMP 2.0 are already implemented
- OpenMP 2.5 – no substantial new features/changes compared to 2.0
- OpenMP 3.0 – task concept added
– new features for loop worksharing
- OpenMP 3.1 – `final` and `mergeable` clauses for `task` construct
– `taskyield` construct to allow user-defined task switching points
– min and max reduction in C/C++
– `OMP_NUM_THREADS` can handle a list for nested regions
– `OMP_PROC_BIND` to bind threads to processors
- OpenMP 4.0 – Thread affinity and `OMP_PLACES`
– SIMD support
– Support for accelerators
– Tasking extensions



OpenMP Information

- OpenMP Homepage: <http://www.openmp.org/>
- OpenMP user group: <http://www.compunity.org/>
- Barbara Chapman, Gabriele Jost, and Ruud van der Pas:
Using OpenMP.
MIT Press, 2008, ISBN-13: 978-0-262-53302-7.
- Georg Hager, Gerhard Wellein:
Introduction to High Performance Computing for Scientists and Engineers.
CRC Press, 2010, 256p, ISBN13: 978-1-439-81192-4
- R.Chandra, L. Dagum, D. Kohr, D. Maydan, J. McDonald, and R. Menon:
Parallel programming in OpenMP.
Academic Press, San Diego, USA, 2000, ISBN 1-55860-671-8
- R. Eigenmann, Michael J. Voss (Eds):
OpenMP Shared Memory Parallel Programming.
Springer LNCS 2104, Berlin, 2001, ISBN 3-540-42346-X

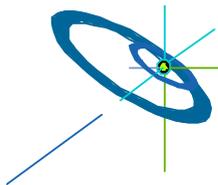


Outline — Programming and Execution Model

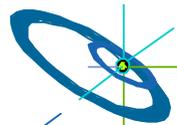
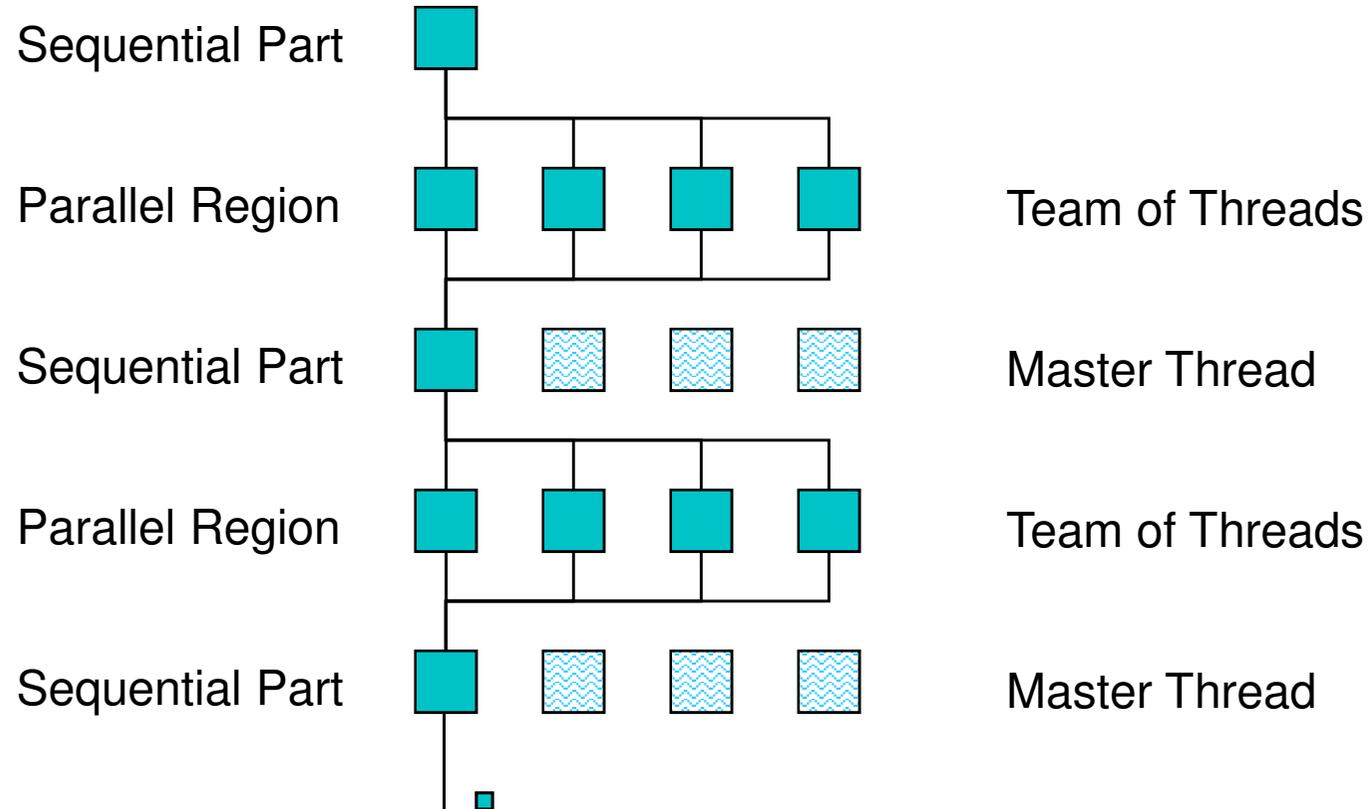
- Introduction into OpenMP
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 - **Parallel regions: team of threads**
 - **Syntax**
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 - **Runtime library routines**
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 - Exercise 2: Pi
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 - Exercise 4: Heat
- Summary of OpenMP API
- OpenMP Pitfalls

OpenMP Programming Model

- OpenMP is a shared memory model.
- Workload is distributed between threads
 - Variables can be
 - **shared among all threads**
 - **duplicated for each thread**
 - Threads communicate by sharing variables.
- Unintended sharing of data can lead to race conditions:
 - race condition: when the program's outcome changes as the threads are scheduled differently.
- To control race conditions:
 - Use synchronization to protect data conflicts.

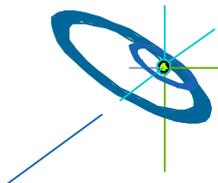


OpenMP Execution Model



OpenMP Execution Model Description

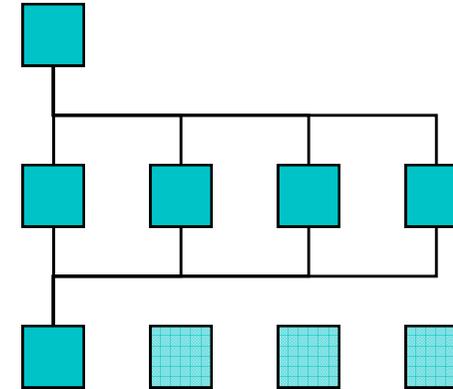
- Fork-join model of parallel execution
- Begin execution as a single process (master thread)
- Start of a parallel construct:
Master thread creates team of threads
- Completion of a parallel construct:
Threads in the team synchronize:
implicit barrier
- Only master thread continues execution



OpenMP Parallel Region Construct

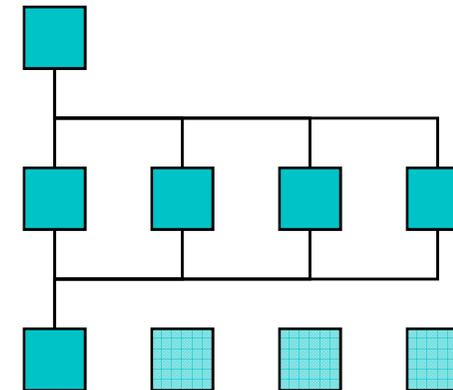
Fortran

Fortran: !\$OMP PARALLEL
 block
 !\$OMP END PARALLEL



C/C++

C / C++: #pragma omp parallel
 structured block
 /* omp end parallel */



OpenMP Parallel Region Construct Syntax

- Block of code to be executed by multiple threads in parallel. Each thread executes the **same code redundantly!**
- Fortran:

```
!$OMP PARALLEL [ clause [ [ , ] clause ] ... ]  
block  
!$OMP END PARALLEL
```

 - parallel/end parallel directive pair must appear in the same routine
- C/C++:

```
#pragma omp parallel [ clause [ [ , ] clause ] ... ] new-line  
structured-block
```
- *clause* can be one of the following:
 - private (*list*)
 - shared (*list*)
 - ...

[xxx] = xxx is optional

Fortran

C/C++

Introduction to OpenMP [07]



OpenMP Directive Format: C/C++

- `#pragma` directives – case sensitive
- Format:
`#pragma omp directive_name [clause [[,] clause] ...] new-line`
- Conditional compilation
`#ifdef _OPENMP`
`block,`
`e.g., printf(“%d avail.processors\n”, omp_get_num_procs());`
`#endif`
- Include file for library routines:
`#ifdef _OPENMP`
`#include <omp.h>`
`#endif`
- In the old OpenMP 1.0 syntax, the comma [,] between clauses was not allowed (some compilers in use still may have this restriction)



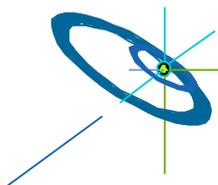
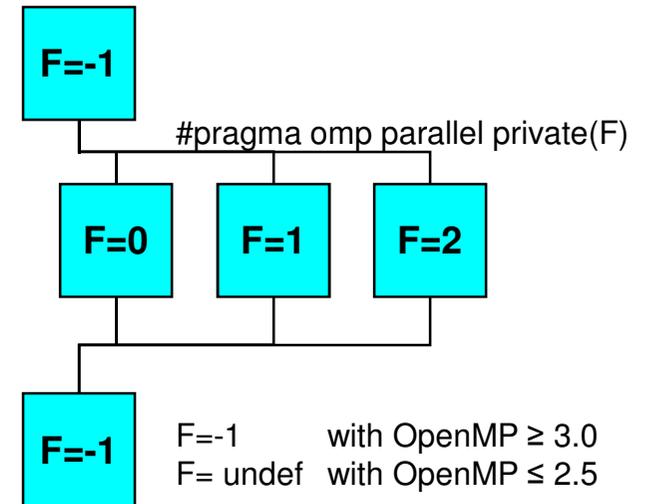
OpenMP Directive Format: Fortran

- Treated as Fortran comments – not case sensitive
- Format:
sentinel directive_name [*clause* [[,] *clause*] ...]
- Directive sentinels:
 - Fixed source form: **!\$OMP** | C\$OMP | *\$OMP [starting at column 1]
 - Free source form: **!\$OMP** [may be preceded by white space]
- Conditional compilation
 - Fixed source form: **!\$** | C\$ | *\$
 - Free source form: **!\$_**
 - #ifdef _OPENMP [in my_fixed_form.F or .F90]
 block
 #endif
 - Example:
 !\$ write(*,*) OMP_GET_NUM_PROCS(), ' avail. processors'
- Include file for library routines:
 - include 'omp_lib.h' or use omp_lib [implementation dependent]

OpenMP Data Scope Clauses

- `private (list)`
Declares the variables in *list* to be private to each thread in a team
- `shared (list)`
Makes variables that appear in *list* shared among all the threads in a team
- If not specified: default `shared`, but
 - stack (local) variables in called sub-programs are PRIVATE
 - Automatic variables within a block are PRIVATE
 - Loop control variable of parallel OMP
 - `DO` (Fortran)
 - `for` (C)is PRIVATE
 - ...

[see later: Data Model]



OpenMP Environment Variables

- OMP_NUM_THREADS
 - sets the number of threads to use during execution
 - when dynamic adjustment of the number of threads is enabled, the value of this environment variable is the maximum number of threads to use
 - `setenv OMP_NUM_THREADS 16` **[csh, tcsh]**
 - `export OMP_NUM_THREADS=16` **[sh, ksh, bash]**
- OMP_SCHEDULE
 - **applies only to `do/for` and `parallel do/for` directives that have the schedule type `RUNTIME`**
 - sets schedule type and chunk size for all such loops
 - `setenv OMP_SCHEDULE "GUIDED, 4"` **[csh, tcsh]**
 - `export OMP_SCHEDULE="GUIDED, 4"` **[sh, ksh, bash]** ■



OpenMP Runtime Library (1)

- Query functions
- Runtime functions
 - Run mode
 - Nested parallelism
- Lock functions
- C/C++: add `#include <omp.h>`
- Fortran: add all necessary OMP routine declarations, e.g.,

C/C++

Fortran

```
!$    INTEGER omp_get_thread_num
```

or use include file

```
!$    INCLUDE 'omp_lib.h'
```

or module

```
!$    USE omp_lib
```

Existence of include file or module or both is implementation dependent.



OpenMP Runtime Library (2)

- `omp_get_num_threads` Function
Returns the number of threads currently in the team executing the parallel region from which it is called
 - Fortran:
`integer function omp_get_num_threads()`
 - C/C++:
`int omp_get_num_threads(void);`
- `omp_get_thread_num` Function
Returns the thread number, within the team, that lies between 0 and `omp_get_num_threads() - 1`, inclusive. The master thread of the team is thread 0

Fortran

C/C++

Fortran

C/C++

OpenMP Runtime Library (3): Wall clock timers **OpenMP 2.0**

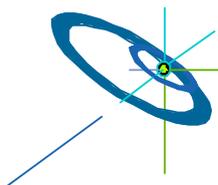
- Portable wall clock timers similar to MPI_WTIME
- DOUBLE PRECISION FUNCTION OMP_GET_WTIME()

- provides elapsed time

```
START=OMP_GET_WTIME()  
! Work to be measured  
END = OMP_GET_WTIME()  
PRINT *, 'Work took ', END-START, ' seconds'
```

- provides “per-thread time”, i.e. needs not be globally consistent

- DOUBLE PRECISION FUNCTION OMP_GET_WTICK()
 - returns the number of seconds between two successive clock ticks



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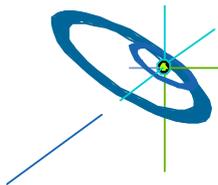


OpenMP Exercise 1: Parallel region (1)

- Goal: usage of
 - runtime library calls
 - conditional compilation
 - environment variables
 - parallel regions, `private` and `shared` clauses
- Working directory: `~/OpenMP/#NR/pi/`
#NR = number of your PC, e.g., 07
- Serial programs:
 - Fortran 77: `pi.f`
 - Fortran 90: `pi.f90`
 - C: `pi.c`

Fortran

C/C++



OpenMP Exercise 1: Parallel region (2)

- compile **serial** program `pi.[f|f90|c]` and run
- compile **as OpenMP** program and run on 4 CPUs
 - add OpenMP compile option, see , e.g.,
 - `-mp` on SGI login slides
 - `-openmp` on Intel compiler `icc` and `ifc`
 - `export OMP_NUM_THREADS=4`
 - `./pi`
 - expected result: program is not parallelized, therefore same pi-value and timing, **additional output from `omp_get_wtime()`**



OpenMP Exercise 1: Parallel region (3)

- Directly after the declaration part, add a **parallel region that prints on each thread**
 - **its rank** (with `omp_get_thread_num()`) and
 - **the number of threads** (with `omp_get_num_threads()`)
- compile and run on 4 CPUs
- Expected results: numerical calculation is still not parallelized, therefore still same pi-value and timing, additionally output:

```
bash$ gcc -openmp -o pi0-parallel pi0.c
bash$ export OMP_NUM_THREADS=4; ./pi0-parallel
I am thread 0 of 4 threads
I am thread 2 of 4 threads
I am thread 3 of 4 threads
I am thread 1 of 4 threads
computed pi = 3.1415926535897931
CPU time (clock) = 0.06734 sec
wall clock time (omp_get_wtime) = 0.06682 sec
wall clock time (gettimeofday) = 0.06683 sec
```

} undefined sequence!



login slides



OpenMP Advanced Exercise 1a: Parallel region (4)

- Use a private variable for the rank of the threads
- Check, whether you can get a race-condition if you forget the `private` clause on the `omp parallel` directive, e.g.:

```
I am thread 2 of 4 threads  
I am thread 2 of 4 threads  
I am thread 2 of 4 threads  
I am thread 2 of 4 threads
```

- Don't wonder if you get always correct output because the compiler may use on each thread a private register instead of writing into the shared memory



login slides



OpenMP Advanced Exercise 1b: Parallel region (5)

- Guarantee with conditional compilation, that source code still works with non-OpenMP compilers (i.e., without OpenMP compile-option).
- Add an “else clause”, printing a text if OpenMP is not used.
- Expected output:
 - If compiled with OpenMP, see previous slide.
 - If compiled without OpenMP:

```
bash$ gcc -o pi0-serial pi0.c
bash$ export OMP_NUM_THREADS=4; ./pi0-serial
This program is not compiled with OpenMP
computed pi =          3.1415926535897931
CPU time (clock)           =          0.06734 sec
wall clock time (gettimeofday) =          0.06706 sec
```



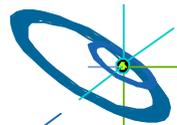
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OpenMP Exercise 1: Parallel region – Solution

Location: `~/OpenMP/solution/pi`

- `pi.[f|f90|c]` original program
- `pi0.[f|f90|c]` solution (includes all 3 exercises)



OpenMP Exercise 1: Summary

- Conditional compilation allows to keep the serial version of the program in the same source files
- compilers need to be used with `special` option for OpenMP directives to take any effect
- Parallel regions are executed by each thread in the same way unless worksharing directives are used
- Decision about `private` or `shared` status of variables is important (Advanced Exercise 1a)



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Worksharing and Synchronization

- Which thread executes which statement or operation?
- and when?
 - Worksharing constructs
 - Master and synchronization constructs
- **i.e., organization of the parallel work!!!**



OpenMP Worksharing Constructs

- Divide the execution of the enclosed code region among the members of the team
- Must be enclosed dynamically within a parallel region
- They do not launch new threads
- No implied barrier on entry
- `sections` directive
- `for` directive (C/C++)
- `do` directive (Fortran)
- `workshare` directive (Fortran)
- `task` directive
- `single` directive

C/C++

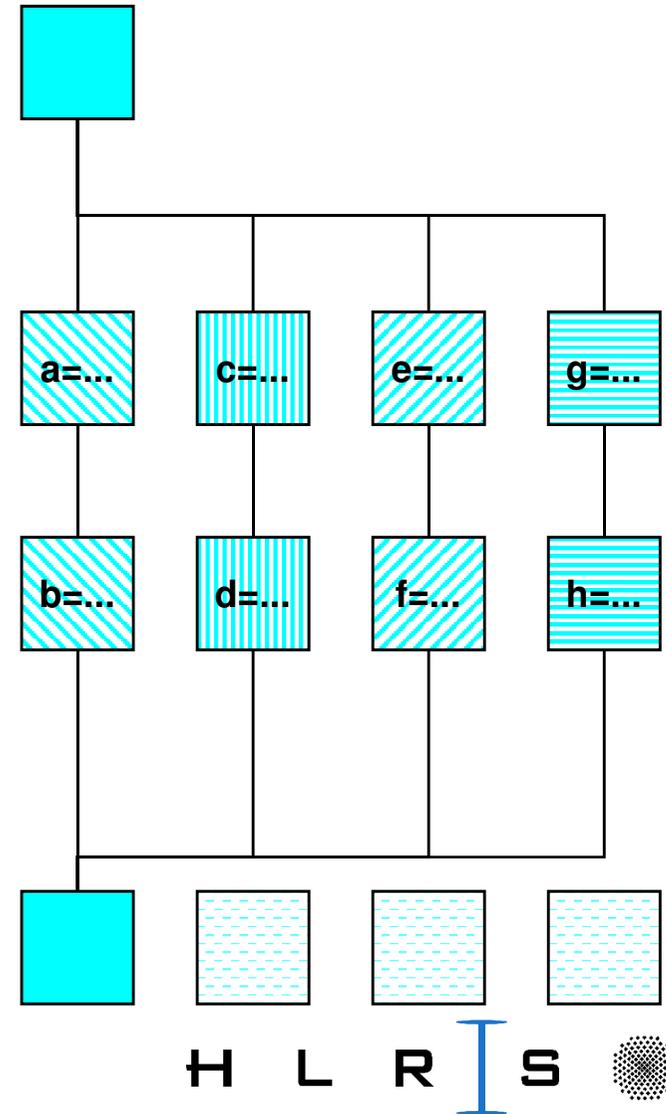
Fortran



```

C / C++:
#pragma omp parallel
{
#pragma omp sections
  {
    a=...;
    b=...;
  }
#pragma omp section
  {
    c=...;
    d=...;
  }
#pragma omp section
  {
    e=...;
    f=...;
  }
#pragma omp section
  {
    g=...;
    h=...;
  }
} /*omp end sections*/
} /*omp end parallel*/

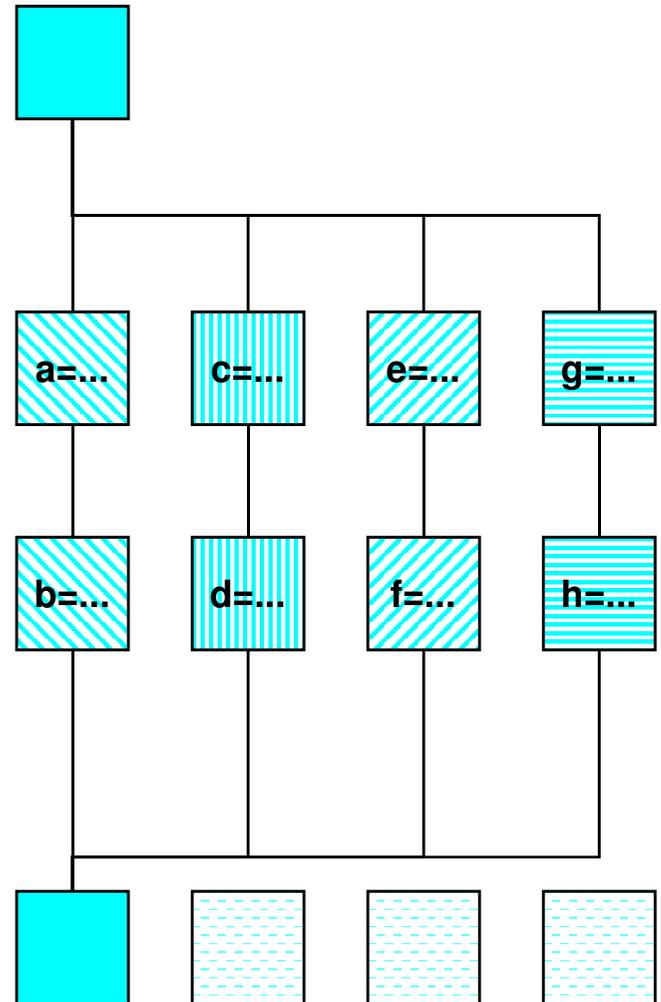
```



Fortran:

```

!$OMP PARALLEL
!$OMP SECTIONS
  a=...
  b=...
!$OMP SECTION
  c=...
  d=...
!$OMP SECTION
  e=...
  f=...
!$OMP SECTION
  g=...
  h=...
!$OMP END SECTIONS
!$OMP END PARALLEL
    
```



H L R | S



OpenMP sections Directives – Syntax

Fortran

- Several *blocks* are executed in parallel

- Fortran:

```
!$OMP SECTION S [ clause [,] clause ] ... ]
```

```
[!$OMP SECTION
```

```
  block1
```

```
[!$OMP SECTION
```

```
  block2 ]
```

```
...
```

```
!$OMP END SECTION S [nowait]
```

Blocks must be independent, i.e., they can be executed in parallel

C/C++

- C/C++:

```
#pragma omp sections [ clause [,] clause ] ... ] new-line
```

```
{
```

```
  [#pragma omp section new-line
```

```
    structured-block1
```

```
  [#pragma omp section new-line
```

```
    structured-block2 ]
```

```
...
```

```
}
```

C / C++:

#pragma omp parallel private(f)

{

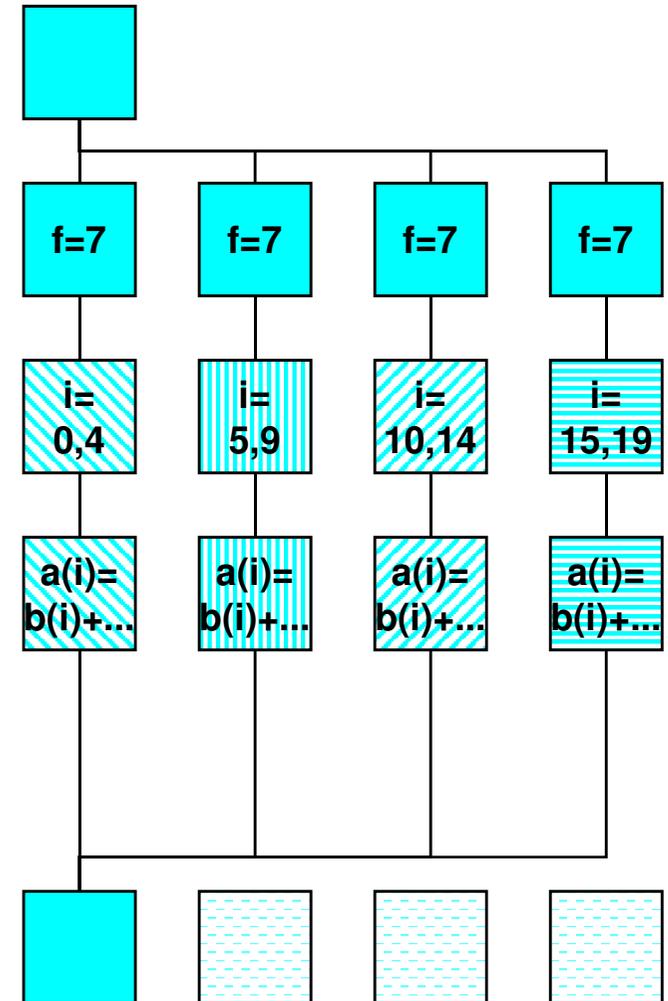
f=7;

#pragma omp for

for (i=0; i<20; i++)

a[i] = b[i] + f * (i+1);

} /* omp end parallel */



H L R I S

Fortran:

!\$OMP PARALLEL private(f)

f=7

!\$OMP DO

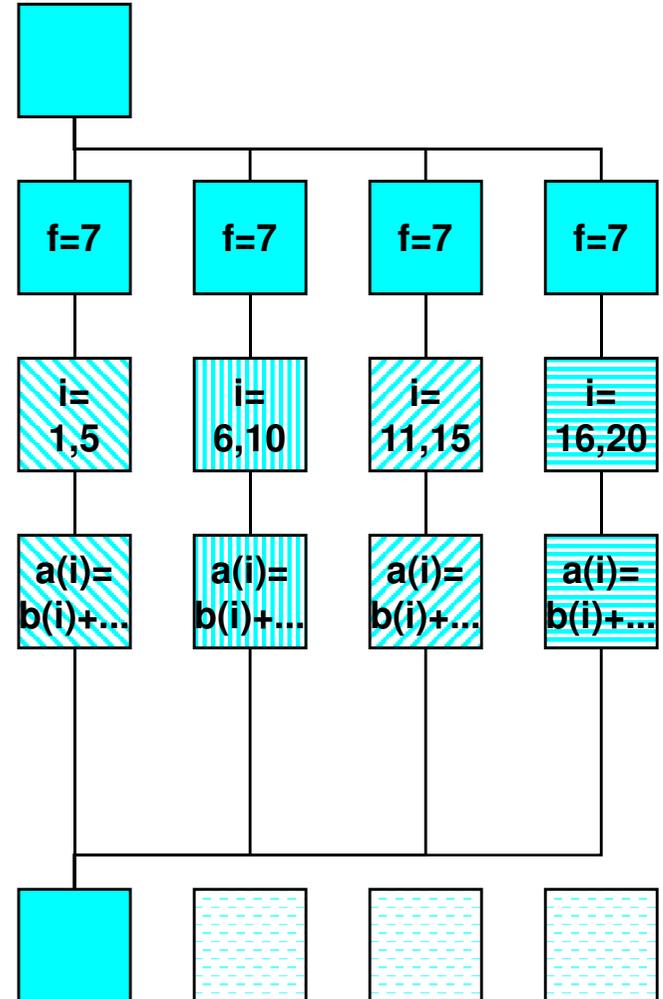
do i=1,20

a(i) = b(i) + f * i

end do

!\$OMP END DO

!\$OMP END PARALLEL



OpenMP do/for Directives – Syntax

Fortran

- Immediately following loop executed in parallel

- Fortran:

```
!$OMP do [ clause [ [ , ] clause ] ... ]  
    do_loop  
[ !$OMP end do [ nowait ] ]
```

Loop iterations must be independent, i.e., they can be executed in parallel

- If used, the `end do` directive must appear immediately after the end of the loop

- C/C++:

```
#pragma omp for [ clause [ [ , ] clause ] ... ] new-line  
    for-loop
```

- The corresponding `for` loop must have *canonical shape*
→ *next slide*

C/C++

OpenMP for Directives – Canonical Shape

Fortran

- C/C++:
`#pragma omp for [clause [[,] clause] ...] new-line
for-loop`

- The corresponding for loop must have *canonical shape*:

```
for( [integer type] var=lb; var < b; var++      )  
    <=    ++var  
    >    var+=incr  
    >=   var=var+incr  
    var-- ...
```

C/C++

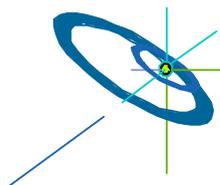
var : must not be modified in the loop body;
integer (signed or unsigned),
or pointer type (C only), ← (OpenMP ≥ 3.0)
or random access iterator type (C++ only)

lb, b, incr : loop invariant expression
→ the number of iterations must be computable at loop begin



OpenMP `do/for` Directives – Details

- *clause* can be one of the following:
 - `private (list)` [see later: Data Model]
 - `reduction (operator: list)` [see later: Data Model]
 - `collapse (n)` (OpenMP \geq 3.0)
 - `schedule (type [, chunk])`
 - `nowait` (C/C++: `on #pragma omp for`)
(Fortran: `on $!OMP END DO`)
 - ...
- Implicit barrier at the end of `do/for` unless `nowait` is specified, i.e., if `nowait` is specified, threads do not synchronize at the end of the parallel loop
- `collapse (n)` with constant integer expression *n*:
The iterations of the following *n* nested loops are collapsed into one larger iteration space.
- `schedule` clause specifies how the iterations (iteration space) of the (nested) loop(s) are divided among the threads of the team.



OpenMP `schedule` Clause

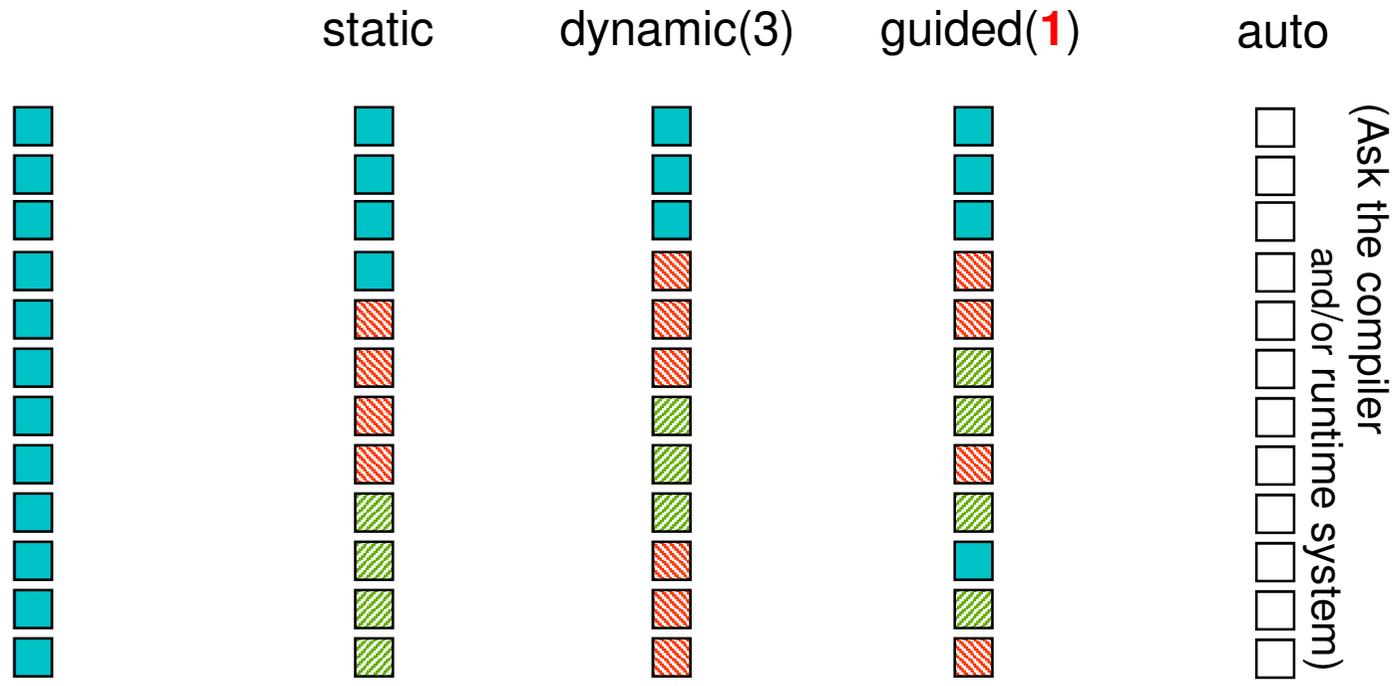
Within `schedule(type [, chunk])` `type` can be one of the following:

- `static`: Iterations are divided into pieces of a size specified by `chunk`. The pieces are statically assigned to threads in the team in a round-robin fashion in the order of the thread number. Default chunk size: one contiguous piece for each thread.
- `dynamic`: Iterations are broken into pieces of a size specified by `chunk`. As each thread finishes a piece of the iteration space, it dynamically obtains the next set of iterations. Default chunk size: 1.
- `guided`: The chunk size is reduced in an exponentially decreasing manner with each dispatched piece of the iteration space. `chunk` specifies the smallest piece (except possibly the last). Default chunk size: 1. Initial chunk size is implementation dependent.
- `auto`: Scheduling is delegated to the compiler and/or runtime system (**OpenMP ≥ 3.0**)
- `runtime`: The decision regarding scheduling is deferred until run time. The schedule type and chunk size can be chosen at run time by setting the `OMP_SCHEDULE` environment variable.

Default schedule: implementation dependent. ■

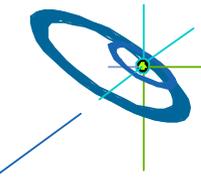


Loop scheduling



• Method is implementation dependent, e.g.,
 13 iterations on 3 threads = 5+5+3 or = 5+4+4
 • Two loops in same parallel region and
 with same count are divided in same way,
 i.e., static schedule is **deterministic**

} **OpenMP ≥ 3.0**



- WORKSHARE directive allows parallelization of array expressions and FORALL statements
- Usage:

```
!$OMP WORKSHARE  
A=B+C  
! Rest of block  
!$OMP END WORKSHARE
```
- Semantics:
 - Work inside block is divided into separate units of work.
 - Each unit of work is executed only once.
 - The units of work are assigned to threads in any manner.
 - The compiler must ensure sequential semantics.
 - Similar to `PARALLEL DO` without explicit loops.



OpenMP task Directive – Example: Parallelized traversing of a tree

OpenMP 3.0

C/C++

```
struct node {
    struct node *left;
    struct node *right;
};
extern void process(struct node *);
void traverse( struct node *p ) {
    if (p->left)
#pragma omp task // p is firstprivate by default
        traverse(p->left);
    if (p->right)
#pragma omp task // p is firstprivate by default
        traverse(p->right);
    process(p); // significant work with p
}
int main(int argc, char **argv)
{ struct node tree;
  ... // producing the tree
#pragma omp parallel
  {
#pragma omp single
  {
      traverse(&tree); //traversing the existing tree
  } // end of omp single
  } // end of omp parallel
}
```

- Starting the parallel team of threads
- Using only one thread for starting the traversal
- First execution with single thread (= 1st task)
- A new task is started (on a new thread)
- A recursive call to traverse() in this 2nd task
- 3rd task is started
- Work is done in 1st task
- Recursive calls starting 4th, 5th, ... tasks

Trick: OpenMP can choose whether new tasks are immediately started or deferred until free thread is available. ■

skipped

OpenMP task Directive – Example: Linked list

OpenMP 3.0

Fortran

```
MODULE LIST
  TYPE NODE
    INTEGER :: PAYLOAD
    TYPE (NODE), POINTER :: NEXT
  END TYPE NODE
CONTAINS
  SUBROUTINE PROCESS(P)
    TYPE (NODE), POINTER :: P
    ! do work here
  END SUBROUTINE
  SUBROUTINE INCREMENT_LIST_ITEMS (HEAD)
    TYPE (NODE), POINTER :: HEAD
    TYPE (NODE), POINTER :: P
    !$OMP PARALLEL PRIVATE(P)
      !$OMP SINGLE
        P => HEAD
        DO
          !$OMP TASK
            ! P is firstprivate by default
            CALL PROCESS(P)
          !$OMP END TASK
          P => P%NEXT
          IF ( .NOT. ASSOCIATED (P) ) EXIT
        END DO
      !$OMP END SINGLE
    !$OMP END PARALLEL
  END SUBROUTINE
END MODULE
```

The **traversal** of the linked list is done **sequentially** by a **single thread**

The parallel tasks are used for **PROCESS(P)**.

firstprivate(p)

- by default
- **necessary** because traversal (in main thread) modifies p.

Rules not very clear
→ make it explicit with **firstprivate(p)** clause on **task** directive

Fortran

- The **task** construct defines an explicit task.

- Fortran:

```
!$OMP task [ clause [ [ , ] clause ] ... ]  
    block  
!$OMP end task
```

C/C++

- C/C++:

```
#pragma omp task [ clause [ [ , ] clause ] ... ] new-line  
    structured-block
```

- Clauses:

- untied
- default(shared | none | private | firstprivate)
- private(*list*)
- firstprivate(*list*)
- shared(*list*)
- if(*scalar expression*)



- When a thread encounters a `task` construct, a task is generated from the code for the associated structured block.
 - The encountering thread
 - may immediately execute the task,
 - or may defer its execution.
- The number of tasks can be limited, e.g., to the number of threads.
- Completion of a task can be guaranteed using task synchronization constructs → `taskwait` construct.
 - When `if(false)` clause exists, then execution is “*serial*”
 - **Task scheduling points:**
 - In the generating task: Immediately following the generation of an explicit task.
 - In the generated task: After the last instruction of the task region.
 - If task is “*untied*”: Everywhere inside of the task.
 - In implicit and explicit barriers.
 - In `taskwait`.

At task scheduling points, tasks can be resumed or suspended.

(Further constraints → OpenMP 3.0, Sect. 2.7.1, page 62)



skipped

OpenMP taskwait Synchronization

OpenMP 3.0

- Specifies a wait on **completion of all child tasks** generated since beginning of the current task.

Fortran

- Fortran:
`!$OMP taskwait`

C/C++

- C/C++:
`#pragma omp taskwait`



skipped
C/C++

OpenMP taskwait Synchronization Parallelized traversing of a tree

OpenMP 3.0

```
struct node {
    struct node *left;
    struct node *right;
};
extern void process(struct node *);
void traverse( struct node *p ) {
    if (p->left)
        #pragma omp task // p is firstprivate by default
        traverse(p->left);
    if (p->right)
        #pragma omp task // p is firstprivate by default
        traverse(p->right);
    #pragma omp taskwait
    process(p); // significant work with p
}
int main(int argc, char **argv)
{ struct node tree;
  ... // producing the tree
#pragma omp parallel
  {
#pragma omp single
    { traverse(&tree); //traversing the existing tree
      } // end of omp single
  } // end of omp parallel
}
```

process (p)
executed only after
traverse
• of **p->left**
• and **p->right**
is finished.

Same example in Fortran: OpenMP 3.0, Exa. A.13.2f, page 179

SparseLU with OpenMP tasks

C/C++

```

1 int sparseLU( ) {
2     int ii, jj, kk ;
3     #pragma omp parallel
4         #pragma omp single nowait
5         for ( kk=0; kk<NB; kk++) {
6             lu0 (A[kk][kk]) ;
7             /* fwd phase */
8             for (jj=kk+1; jj<NB; jj++)
9                 if (A[kk][jj] != NULL)
10                    #pragma omp task
11                        fwd(A[kk][kk], A[kk][jj]);
12             /* bdiv phase */
13             for (ii=kk+1; ii<NB; ii++)
14                 if (A[ii][kk] != NULL)
15                    #pragma omp task
16                        bdiv(A[kk][kk], A[ii][kk]);
17             #pragma omp taskwait
18             /* bmod phase */
19             for (ii=kk+1; ii<NB; ii++)
20                 if (A[ii][kk] != NULL)
21                     for (jj=kk+1; jj<NB; jj++)
22                         if (A[kk][jj] != NULL)
23                             #pragma omp task
24                                 {
25                                     if (A[ii][jj]==NULL) A[ii][jj]= allocate_clean_block();
26                                     bmod(A[ii][kk], A[kk][jj], A[ii][jj]);
27                                 }
28             #pragma omp taskwait
29         }
30 }

```

Alternative:

- Using dynamic schedule
- Inefficient due to sparseness
- Using inner loop instead of outer loop will cause higher parallelization overhead, but better load balance

Tasks:

- Tasks are only generated if entry is not empty, i.e., if some work must be done

OpenMP `single` Directive – Syntax

Fortran

- The block is executed by only one thread in the team (not necessarily the master thread)

- Fortran:

```
!$OMP single [ clause [ [ , ] clause ] ... ]
```

```
    block
```

```
!$OMP end single [nowait]
```

- C/C++:

```
#pragma omp single [ clause [ [ , ] clause ] ... ] new-line  
    structured-block
```

- Implicit barrier at the end of **single** construct (unless a **nowait** clause is specified)
- To reduce the fork-join overhead, one can combine
 - several parallel parts (`for`, `do`, `workshare`, `sections`)
 - and sequential parts (`single`)in **one** parallel region (`parallel ... end parallel`)

Outline — Synchronization constructs

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OpenMP Synchronization

- Implicit Barrier
 - beginning and end of `parallel` constructs
 - end of all other control constructs
 - implicit synchronization can be removed with `nowait` clause
- Explicit
 - `critical`
 - ...



OpenMP `critical` Directive

- Enclosed code
 - executed by all threads, but
 - **restricted to only one thread at a time**
- Fortran:

```
!$OMP CRITICAL [ ( name ) ]  
    block  
!$OMP END CRITICAL [ ( name ) ]
```
- C/C++:

```
#pragma omp critical [ ( name ) ] new-line  
    structured-block
```
- A thread waits at the beginning of a critical region until no other thread in the team is executing a critical region with the same name. All unnamed `critical` directives map to the same unspecified name.

Fortran

C/C++

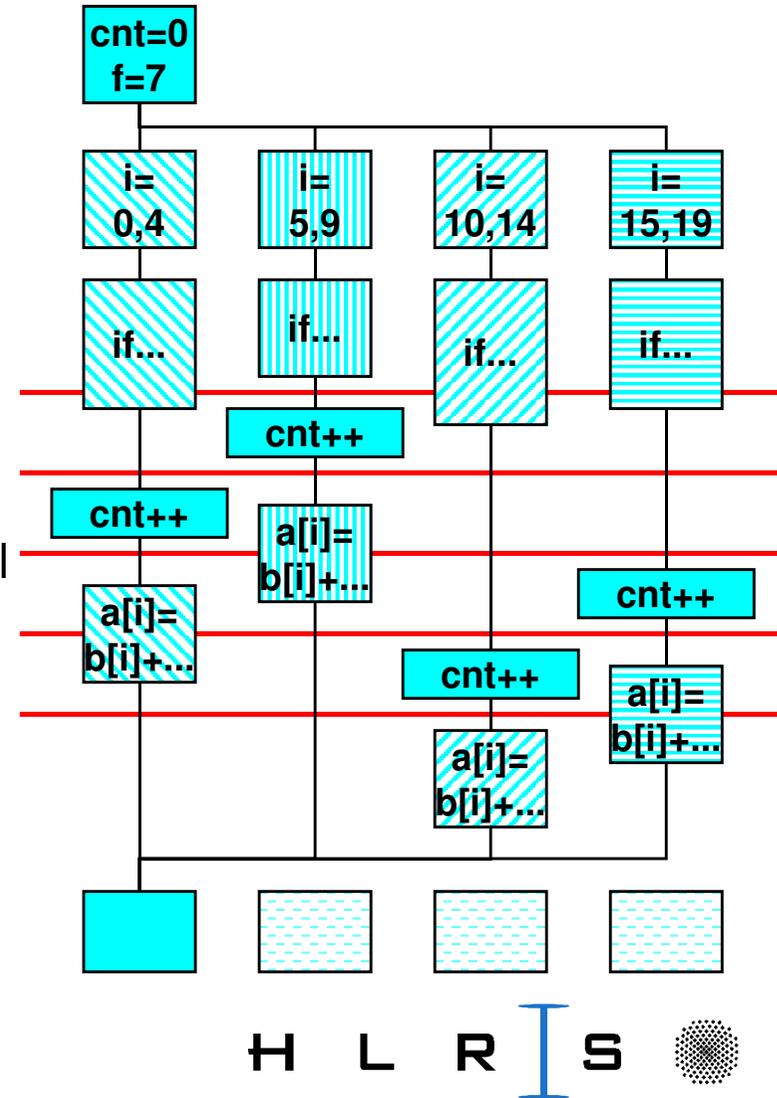
Introduction to OpenMP [07]



OpenMP `critical` — an example (C/C++)

```

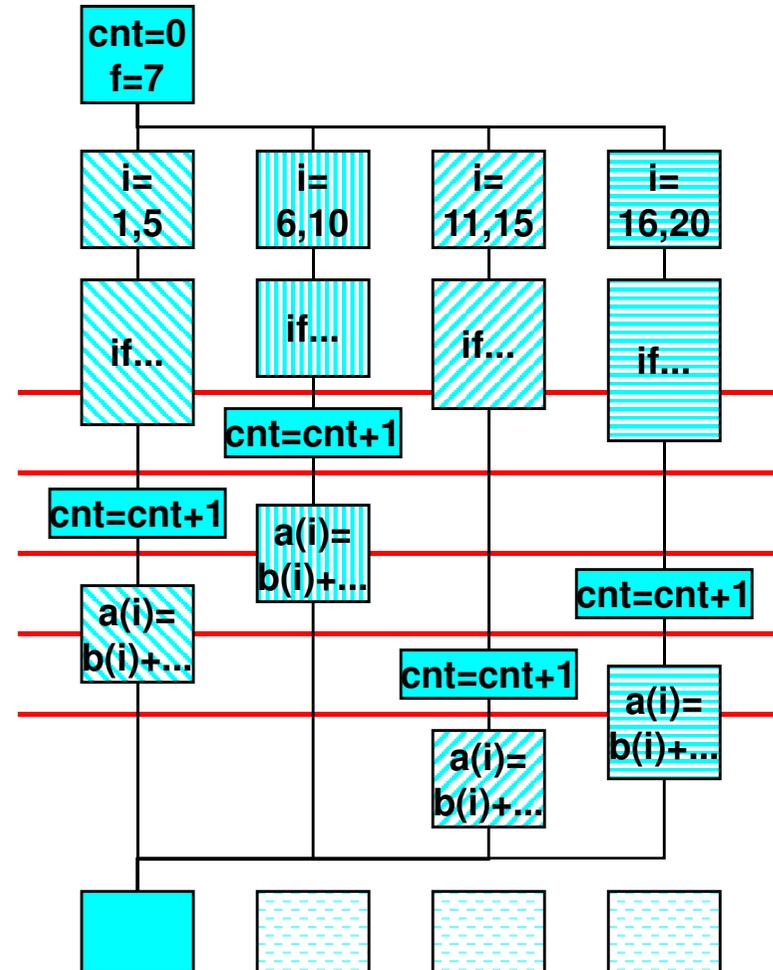
C / C++:  cnt = 0;
          f=7;
          #pragma omp parallel
          {
          #pragma omp for
          for (i=0; i<20; i++) {
            if (b[i] == 0) {
              #pragma omp critical
              cnt ++;
            } /* endif */
            a[i] = b[i] + f * (i+1);
          } /* end for */
        } /*omp end parallel */
  
```



OpenMP `critical` — an example (Fortran)

```

Fortran:  cnt = 0
          f=7
          !$OMP PARALLEL
          !$OMP DO
            do i=1,20
              if (b(i).eq.0) then
                !$OMP CRITICAL
                  cnt = cnt+1
                !$OMP END CRITICAL
              endif
              a(i) = b(i) + f * i
            end do
          !$OMP END DO
          !$OMP END PARALLEL
    
```

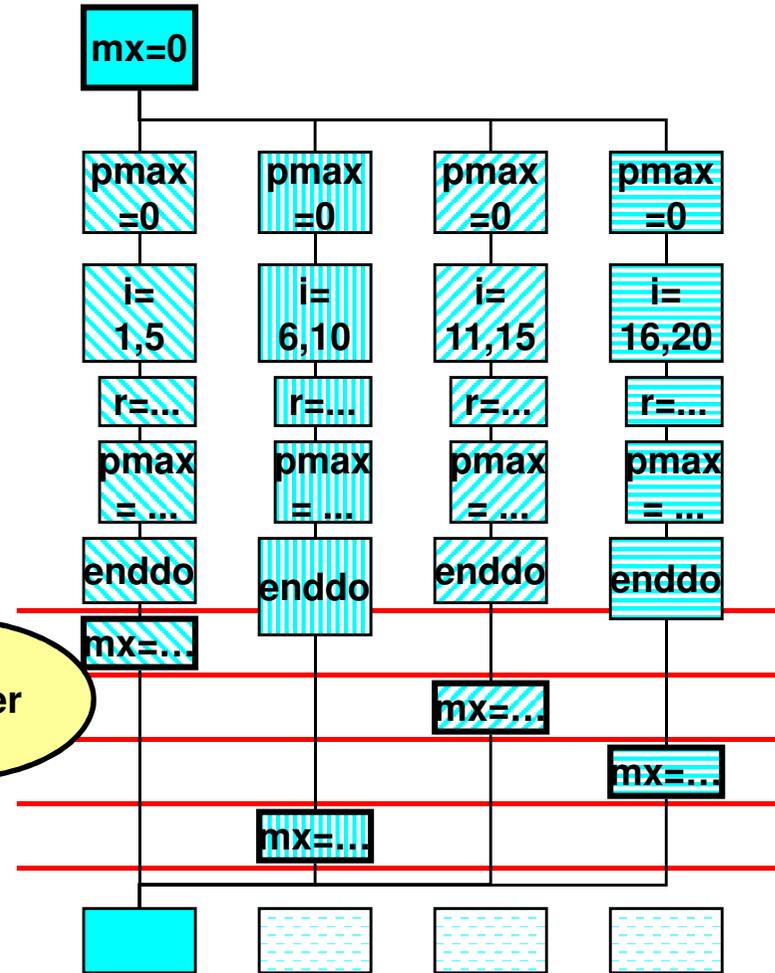


OpenMP `critical` — another example (Fortran)

```

mx = 0
!$OMP PARALLEL private(pmax)
  pmax = 0 ! or most negative number
!$OMP DO private(r)
  do i=1,20
    r = work(i)
    pmax = max(pmax,r)
  end do
!$OMP END DO NOWAIT
!$OMP CRITICAL
  mx = max(mx,pmax)
!$OMP END CRITICAL
!$OMP END PARALLEL
  
```

Only once per thread



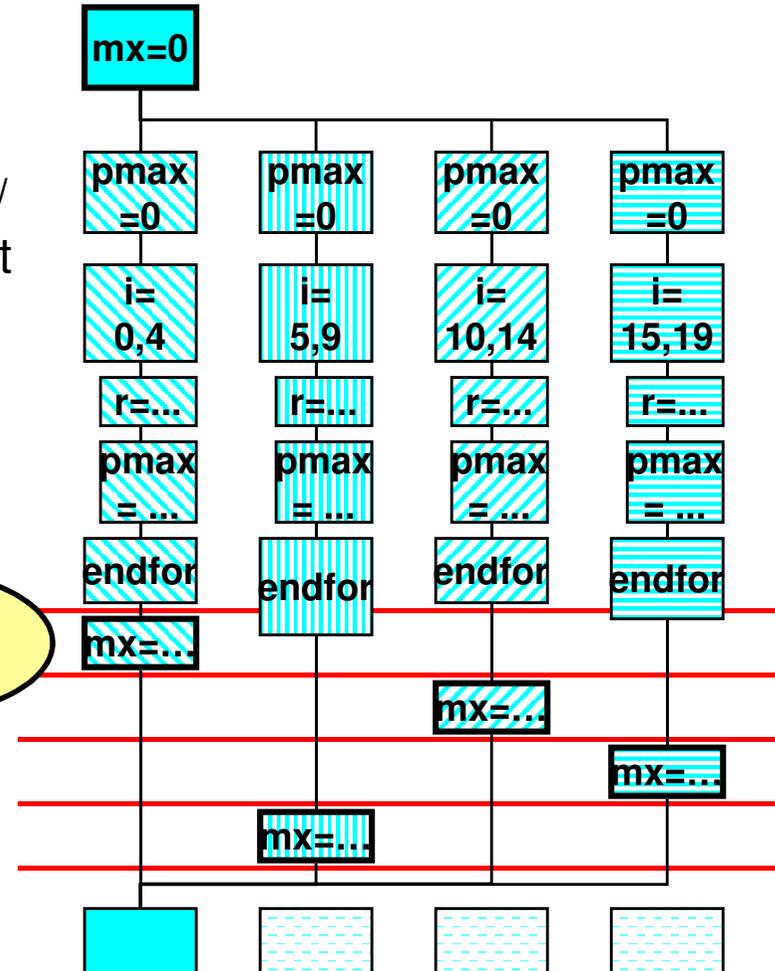
OpenMP `critical` — another example (C/C++)

```

mx = 0;
#pragma omp parallel private(pmax)
{
  pmax = 0; /* or most negative number */
  #pragma omp for private(r) nowait
  for (i=0; i<20; i++)
  {
    r = work(i);
    pmax = (r>pmax ? r : pmax);
  } /*end for*/
  /*omp end for*/
  #pragma omp critical
  mx = (pmax>mx ? pmax : mx);
  /*omp end critical*/
} /*omp end parallel*/

```

Only
once per
thread



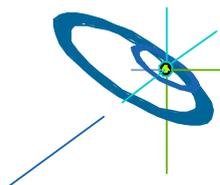
Outline — Nesting and Binding

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OpenMP Vocabulary

- **Static extent** of the parallel construct:
statements enclosed lexically within the construct
- **Dynamic extent** of the parallel construct:
further includes the routines called from within the construct
- **Orphaned Directives:**
Do not appear in the lexical extent of the parallel construct but lie in the dynamic extent
 - Parallel constructs at the top level of the program call tree
 - Directives in any of the called routines

[The terms *lexical extent* and *dynamic extent* are no longer used in OpenMP 2.5,
but still helpful to explain the complex impact of OpenMP directives.]



OpenMP Vocabulary

```
program a
!$OMP PARALLEL
call b
call c
!$OMP END PARALLEL
call d
stop
end
```

Static Extent

```
subroutine b
!$OMP DO
do i=1,n
...
enddo
!$OMP END DO
return
end
subroutine c
return
end
```

Dynamic Extent

Orphaned Directives



OpenMP Control Structures — Summary

- Parallel region construct
 - parallel
- Worksharing constructs
 - sections
 - for (C/C++)
 - do (Fortran)
 - workshare (Fortran)
 - task
 - single
- Combined parallel worksharing constructs [see later]
 - parallel for (C/C++)
 - parallel do (Fortran)
 - parallel workshare (Fortran)
- Synchronization constructs
 - critical

C/C++

Fortran

C/C++

Fortran

Introduction to OpenMP [07]



Outline — Exercise 2: pi

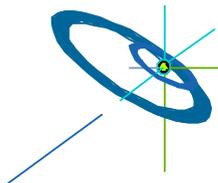
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OpenMP Exercise 2: pi Program (1)

- Goal: usage of
 - worksharing constructs: `do/for`
 - `critical` directive
- Working directory: `~/OpenMP/#NR/pi/`
#NR = number of your PC, e.g., 07
- Serial programs:
 - Fortran 77: `pi.f`
 - Fortran 90: `pi.f90`
 - C: `pi.c`
- Use your result `pi.[f|f90|c]` from the exercise 1
- or copy solution of exercise 1 to your directory:
 - `cp ~/OpenMP/solution/pi/pi0.* .`

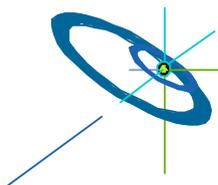
Fortran

C/C++



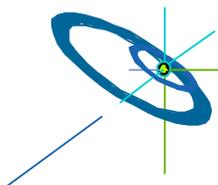
OpenMP Exercise 2: pi Program (2)

- compile serial program `pi.[f|f90|c]` and run
- add parallel region and `do/for` directive in `pi.[f|f90|c]` and compile
- set environment variable `OMP_NUM_THREADS` to 2 and run
 - value of pi? (should be wrong!)
- run again
 - value of pi? (...wrong and unpredictable)
- set environment variable `OMP_NUM_THREADS` to 4 and run
 - value of pi? (...and stays wrong)
- run again
 - value of pi? (...but where is the race-condition?)



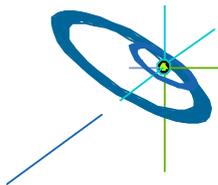
OpenMP Exercise 2: pi Program (3)

- add `private(x)` clause in `pi.[f|f90|c]` and compile
- set environment variable `OMP_NUM_THREADS` to 2 and run
 - value of pi? (should be still incorrect ...)
- run again
 - value of pi?
- set environment variable `OMP_NUM_THREADS` to 4 and run
 - value of pi?
- run again
 - value of pi? (... and where is the second race-condition?)



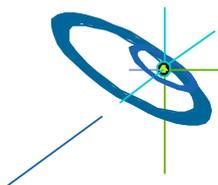
OpenMP Exercise 2: pi Program (4)

- add `critical` directive in `pi.[f|f90|c]` around the sum-statement and compile
- set environment variable `OMP_NUM_THREADS` to 2 and run
 - value of pi? (should be now correct!, but huge CPU time!)
- run again
 - value of pi? (but not reproducible in the last bit!)
- set environment variable `OMP_NUM_THREADS` to 4 and run
 - value of pi? execution time? (Oh, does it take longer?)
- run again
 - value of pi? execution time?
 - How can you optimize your code?



OpenMP Exercise 2: pi Program (5)

- move `critical` directive in `pi.[f|f90|c]` outside loop, restore old iteration length (10,000,000) and compile
- set environment variable `OMP_NUM_THREADS` to 2 and run
 - value of pi?
- run again
 - value of pi?
- set environment variable `OMP_NUM_THREADS` to 4 and run
 - value of pi? execution time? (correct pi, half execution time)
- run again
 - value of pi? execution time?

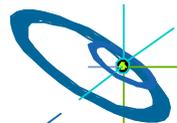


OpenMP Advanced Exercise 2: pi Program (5)

- Modify the printing of the thread rank and the number of threads from Exercise 1:
 - Only one thread should print the real number of threads used in parallel regions.
 - For this, use a `single` construct
 - Expected result:

OpenMP-parallel with 4 threads

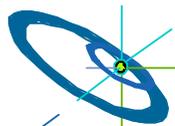
```
computed pi =          3.14159265358967
CPU time (clock) =          0.01659 sec
wall clock time (omp_get_wtime) =      0.01678 sec
wall clock time (gettimeofday) =      0.01679 sec
```



OpenMP Exercise 2: pi Program - Solution

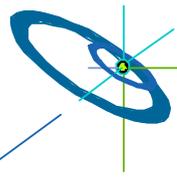
Location: `~/OpenMP/solution/pi`

- `pi.[f|f90|c]` original program
- `pi1.[f|f90|c]` incorrect (no private, no synchronous global access) !!!
- `pi2.[f|f90|c]` incorrect (still no synchronous global access to `sum`) !!!
- `pic.[f|f90|c]` solution with `critical` directive, but extremely slow!
- `pic2.[f|f90|c]` solution with `critical` directive outside loop



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OpenMP Data Scope Clauses

- `private (list)`
Declares the variables in *list* to be private to each thread in a team
- `shared (list)`
Makes variables that appear in *list* shared among all the threads in a team
- If not specified: default `shared`
- Exceptions: `private`
 - stack (local) variables in called subroutines
 - Automatic variables within a block
 - Loop control variable of parallel DO (Fortran) and FOR (C) loops
 - Fortran only:
 - Loop control variable of a sequential loop enclosed in a parallel or task construct
 - Implied-do and forall indices
- Recommendation for C/C++:
 - Avoid private variables, use variables local to a block instead ■

Private Clause

- `private (variable)` creates a local incarnation of the variable for each thread
 - value is uninitialized
 - private copy is not storage associated with the original

```
program wrong
  JLAST = -777
  !$OMP PARALLEL DO PRIVATE(JLAST)
  DO J=1,1000
    ...
    JLAST = J
  END DO
  !$OMP END PARALLEL DO
  print *, JLAST
```

→ writes -777 (OpenMP ≥ 3.0)
or undefined value (OpenMP ≤ 2.5)

- If initialization is necessary use `firstprivate(var)`
- If value is needed after loop use `lastprivate(var)`
 - `var` is updated by the thread that computes
 - the sequentially last iteration (on `do` or `for` loops)
 - the last section
- Nested `private(var)` with same `var` → allocates again new private storage
- Sometimes `shared/private` is undefined → see OpenMP 3.0, Example A.30.2c/f pp. 234-235

OpenMP reduction Clause

- `reduction (operator: list)`
- Performs a reduction on the variables that appear in *list*, with the operator *operator*
- *operator*: one of
 - Fortran:
`+, *, -, .and., .or., .eqv., .neqv., max, min, iand, ior, or ieor`
 - C/C++:
`+, *, -, &, ^, |, &&, or ||`
With OpenMP 3.1 and later: `max, min`
- Variables must be `shared` in the enclosing context
- With OpenMP 2.0 and later, variables can be arrays (Fortran)
- At the end of the `reduction`, the shared variable is updated to reflect the result of combining the original value of the shared reduction variable with the final value of each of the private copies using the operator specified ■

Fortran

C/C++



OpenMP reduction — an example (Fortran)

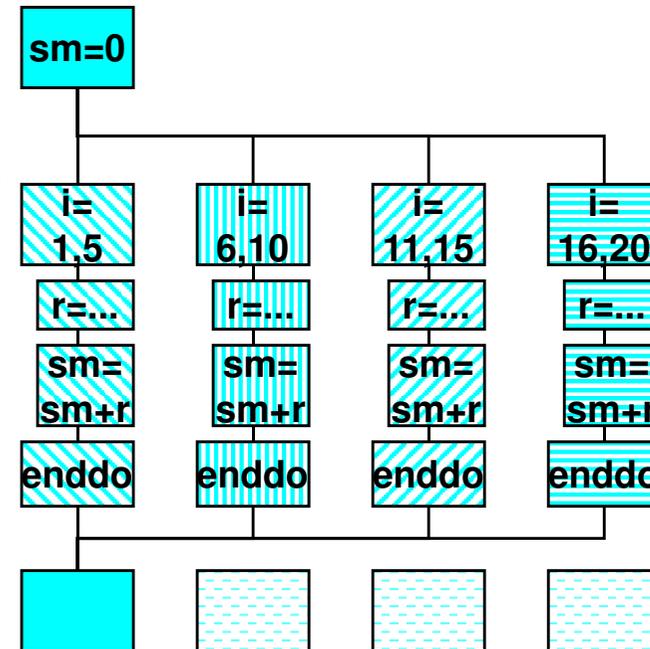
Fortran:

```

sm = 0
!$OMP PARALLEL DO private(r),
reduction(+:sm)

  do i=1,20
    r = work(i)
    sm = sm + r
  end do
!$OMP END PARALLEL DO

```



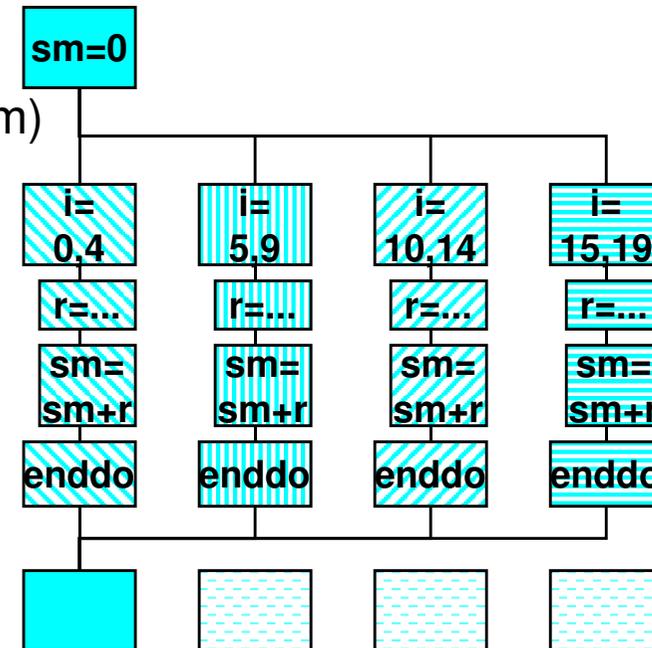
OpenMP reduction — an example (C/C++)

C / C++:

```

sm = 0;
#pragma omp parallel for reduction(+:sm)
for( i=0; i<20; i++)
{ double r;
  r = work(i);
  sm = sm + r ;
} /*end for*/
/*omp end parallel for*/

```



OpenMP Combined `parallel do/for` Directive

Fortran

- Shortcut form for specifying a parallel region that contains a single `do/for` directive

- Fortran:

```
!$OMP PARALLEL DO [ clause [ [ , ] clause ] ... ]  
    do_loop  
[ !$OMP END PARALLEL DO ]
```

C/C++

- C/C++:

```
#pragma omp parallel for [ clause [ clause ] ... ] new-line  
    for-loop
```

- This directive admits all the clauses of the `parallel` directive and the `do/for` directive except the `nowait` clause, with identical meanings and restrictions

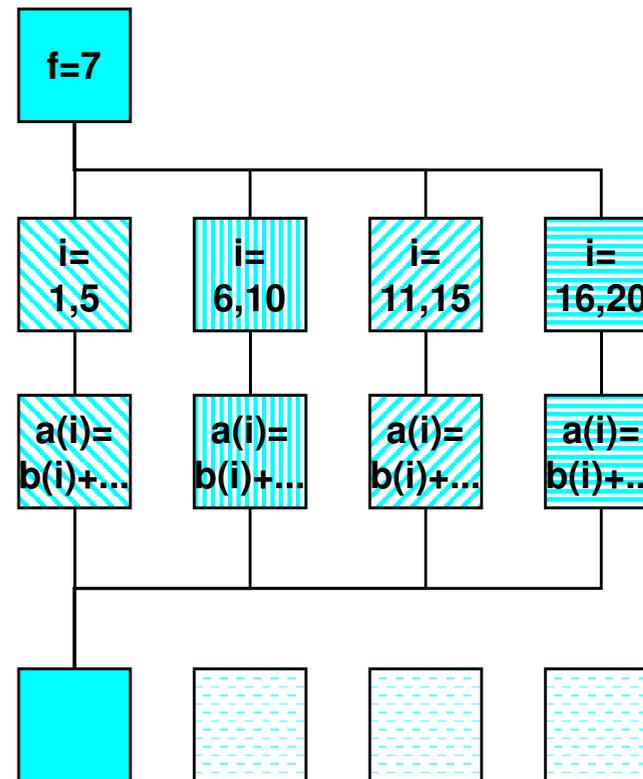


OpenMP Combined parallel do/for — an example (Fortran)

Fortran:

```

f=7
!$OMP PARALLEL DO
do i=1,20
    a(i) = b(i) + f * i
end do
!$OMP END PARALLEL DO
    
```



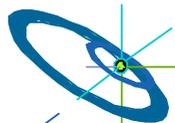
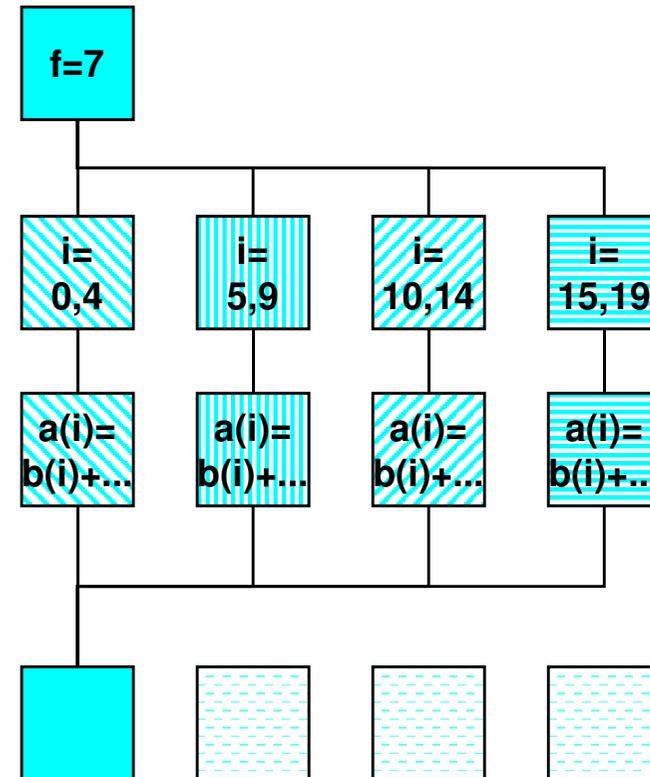
C/C++

OpenMP Combined parallel do/for — an example (C/C++)

C / C++:

f=7;

```
#pragma omp parallel for  
for (i=0; i<20; i++)  
    a[i] = b[i] + f * (i+1);
```

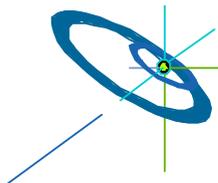


Outline — Exercise 3: pi with reduction

- Introduction into OpenMP
- Programming and Execution Model
 - Parallel regions: team of threads
 - Syntax
 - Data environment (part 1)
 - Environment variables
 - Runtime library routines
 - Exercise 1: Parallel region / library calls / privat & shared variables
- Worksharing directives
 - Which thread executes which statement or operation?
 - Synchronization constructs, e.g., critical regions
 - Nesting and Binding
 - Exercise 2: Pi
- **Data environment and combined constructs**
 - Private and shared variables, Reduction clause
 - Combined parallel worksharing directives
 - **Exercise 3: Pi with reduction clause and combined constructs**
 - **Exercise 4: Heat**
- Summary of OpenMP API
- OpenMP Pitfalls

OpenMP Exercise 3: pi Program (6)

- Goal: usage of
 - worksharing constructs: `do/for`
 - `critical` directive
 - reduction clause
 - combined parallel worksharing constructs:
`parallel do/parallel for`
- Working directory: `~/OpenMP/#NR/pi/`
#NR = number of your PC, e.g., 07
- Use your result `pi.[f|f90|c]` from the exercise 2
- or copy solution of exercise 2 to your directory:
 - `cp ~/OpenMP/solution/pi/pic2.* .`



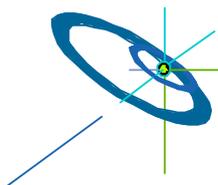
OpenMP Exercise 3: pi Program (7)

- remove `critical` directive in `pi.[f|f90|c]`, add `reduction` clause and compile
- set environment variable `OMP_NUM_THREADS` to 2 and run
 - value of pi?
- run again
 - value of pi?
- set environment variable `OMP_NUM_THREADS` to 4 and run
 - value of pi? execution time?
- run again
 - value of pi? execution time?



OpenMP Exercise 3: pi Program (8)

- change parallel region + `do/for` to the combined parallel worksharing construct `parallel do/parallel for` and compile
- set environment variable `OMP_NUM_THREADS` to 2 and run
 - value of pi?
- run again
 - value of pi?
- set environment variable `OMP_NUM_THREADS` to 4 and run
 - value of pi?
- run again
 - value of pi?
- At the end, compile again **without** OpenMP
 - Does your code still compute a **correct** value of pi?



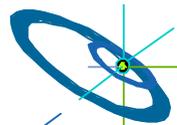
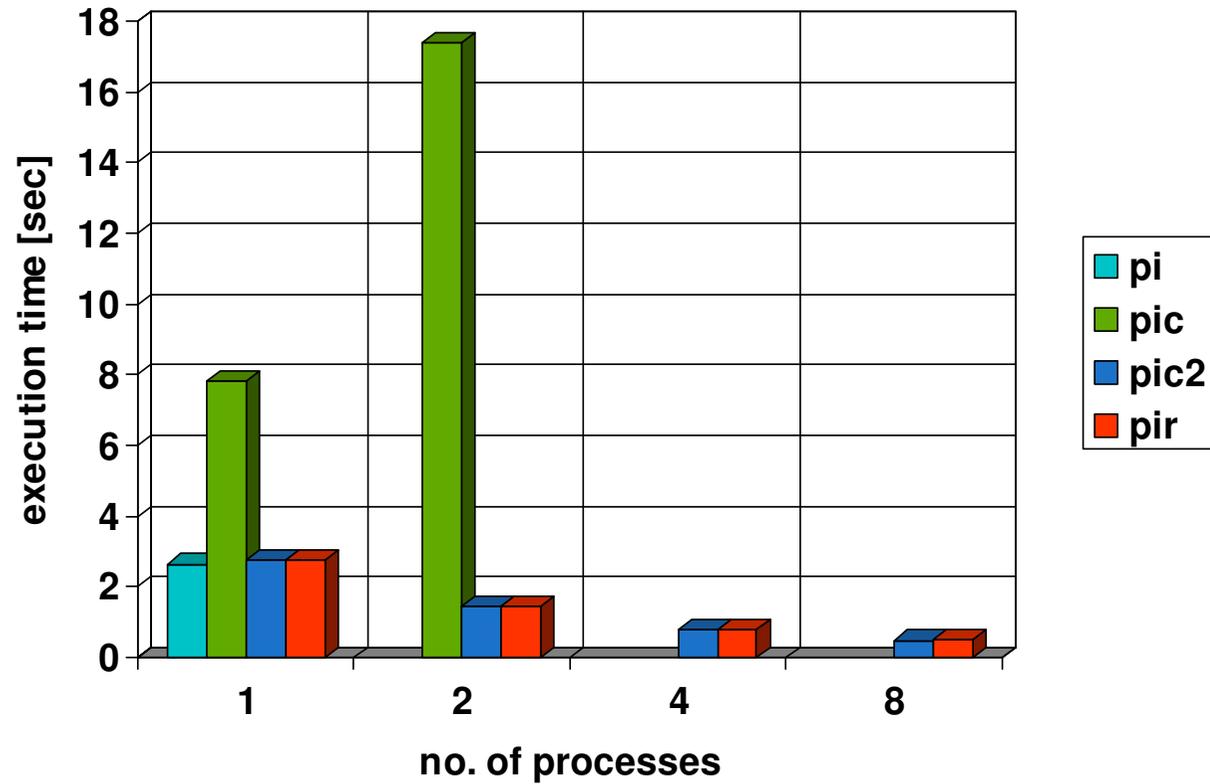
OpenMP Exercise 3: pi Program - Solution

Location: `~/OpenMP/solution/pi`

- `pi.[f|f90|c]` original program
- `pi1.[f|f90|c]` incorrect (no private, no synchronous global access) !!!
- `pi2.[f|f90|c]` incorrect (still no synchronous global access to `sum`) !!!
- `pic.[f|f90|c]` solution with `critical` directive, but extremely slow!
- `pic2.[f|f90|c]` solution with `critical` directive outside loop
- `pir.[f|f90|c]` solution with `reduction` clause

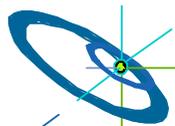


OpenMP Exercise 3: pi Program - Execution Times F90



OpenMP Exercise 3: pi Program - Summary

- Decision about `private` or `shared` status of variables is important
- Correct results with `reduction` clause and with `critical` directive
- Using the simple version of the `critical` directive is much more time consuming than using the `reduction` clause \Rightarrow no parallelism left
- More sophisticated use of `critical` directive leads to much better performance
- Convenient `reduction` clause
- Convenient shortcut form



Outline — Exercise 4: Heat

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 - Syntax
 - Data environment (part 1)
 - Environment variables
 - Runtime library routines
 - Exercise 1: Parallel region / library calls / privat & shared variables
- Worksharing directives
 - Which thread executes which statement or operation?
 - Synchronization constructs, e.g., critical regions
 - Nesting and Binding
 - Exercise 2: Pi
- **Data environment and combined constructs**
 - **Private and shared variables, Reduction clause**
 - **Combined parallel worksharing directives**
 - **Exercise 3: Pi with reduction clause and combined constructs**
 - **Exercise 4: Heat Conduction Exercise**
- Summary of OpenMP API
- OpenMP Pitfalls

OpenMP Exercise: Heat Conduction(1)

- solves the PDE for unsteady heat conduction $df/dt=\Delta f$
- uses an explicit scheme: forward-time, centered-space
- solves the equation over a unit square domain
- initial conditions: $f=0$ everywhere inside the square
- boundary conditions: $f=x$ on all edges
- number of grid points: 20x20



OpenMP Exercise: Heat Conduction (2)

- Goals:
 - parallelization of a real application
 - usage of different parallelization methods with respect to their effect on execution times
- Working directory: `~/OpenMP/#NR/heat/`
#NR = number of your PC, e.g., 07
- Serial programs:
 - Fortran: `heat.F`
 - C: `heat.c`
- Compiler calls:
 - See login slides
- Options:
 - O4 -Dimax=80 -Dkmax=80 (default is 20x20)
 - O4 -Dimax=250 -Dkmax=250
 - O4 -Dimax=1000 -Dkmax=1000 -Ditmax=500

Fortran

C/C++



OpenMP Exercise: Heat Conduction (3)

Tasks:

TODO

Parallelize heat.c or heat.F

- Use critical sections for global maximum: Use trick with partial maximum inside of the parallelized loop, and critical section outside of the loop to compute global maximum
- Or just with: `reduction(max:dphimax)`
- Hints:
 - **Parallelize outer loop (index i in Fortran, k in C)**
 - **make inner loop index private!**

TODO

Compile and run with 80x80 serial, and parallel with 1, 2, 3, 4 threads

- Result may look like
Serial: 0.4 sec, 1 thread: 0.5 sec, 2 threads: **2.8 sec**, ...
- Why is the parallel version significantly slower than the serial one? ■



OpenMP Exercise: Heat Conduction (4)

- Reason already in the **serial** program:
 - Bad sequence of the nested loops

```
do i=1,imax-1
  do k=1,kmax-1
    dphi = (phi(i+1,k)+phi(i-1,k)-2.*phi(i,k))*dy2i
          + (phi(i,k+1)+phi(i,k-1)-2.*phi(i,k))*dx2i
    ! ...
  enddo
enddo
```

Fortran

```
for (k=1;k<kmax;k++)
{ for (i=1;i<imax;i++)
  { dphi=(phi[i+1][k]+phi[i-1][k]-2.*phi[i][k])*dy2i
    + (phi[i][k+1]+phi[i][k-1]-2.*phi[i][k])*dx2i;
    /*...*/
  }
}
```

C/C++

Automatically fixed by serial compiler!

Not fixed by OpenMP compiler!

- Inner loop should use contiguous index in the array, i.e.,
 - First index in Fortran → “do i=...” must be inner loop
 - Second index in C/C++ → “for (k=...)” must be inner loop

Fortran

C/C++

Fortran

C/C++

OpenMP Exercise: Heat Conduction (5)

TODO

Interchange sequence of nested loops for **i** and **k**

Don't forget to modify name of private inner loop index!!!

TODO

Compile and run parallel with 80x80 and with 1, 2, 3, 4 threads

- Result may look like
 - 1 thread: 0.5 sec, 2 threads: **0.45 sec**, 3 threads: **0.40 sec**
- Reasons:
 - Problem is too small — parallelization overhead too large

TODO

Compile and run parallel with 250x250 and with 1, 2, 3, 4 threads

- 1 thread: 4.24 sec, 2 threads: **2.72 sec**, 3 threads: **2.27 sec**
- Don't worry that computation is prematurely finished by `itmax=15000`

TODO

With 1000x1000 and `-Ditmax=500` and with 1, 2, 3, 4 threads

- 1 thread: 5.96 sec, 2 threads: 2.79 sec, 3 threads: **1.35 sec**
- **Super-linear speed-up** due to better cache reuse on smaller problem



OpenMP Exercise: Heat Conduction (6)

Advanced exercise

- Substitute

- TO DO** – the current parallel region that is forked and joined in each `it=...` iteration
- by a parallel region around `it=...` loop forked and joined only once

- Caution:

- TO DO** – `dphimax=0` must be surrounded by

```
#pragma omp barrier
#pragma omp single
{ dphimax=0;
}
```
- Why?

Shared(dphimax) is necessary for B.
Write-write-conflict on A-A without single.
Write-read-conflict on A-B without barrier.

```
/*time step iteration */
for (it=1;it<=itmax;it++)
{
  dphimax=0.; /*line A*/

  for (k=1;k<kmax;k++) worksharing
  {
    for (i=1;i<imax;i++)
    {
      dphi=(phi[i+1][k]+phi[i-1][k]-2.*phi[i][k])*dy2i
        +(phi[i][k+1]+phi[i][k-1]-2.*phi[i][k])*dx2i;
      dphi=dphi*dt;
      dphimax=max(dphimax,dphi);
      phin[i][k]=phi[i][k]+dphi;
    }
  }

  for (k=1;k<kmax;k++) worksharing
  {
    for (i=1;i<imax;i++)
    {
      phi[i][k]=phin[i][k];
    }
  }

  if(dphimax<eps) break; /*line B*/
}
}
```

OpenMP Exercise: Heat Conduction (7)

Advanced exercise

TODO

Execute abort-statement (`if (dphimax<eps) ...`)
only each 20th `it=...` iteration

Move `omp barrier` directly after `if (dphimax<eps) ...`
that this barrier is also executed only each 20th `it=...` iteration

TODO

Add `schedule(runtime)` and compare execution time

Fortran

TODO

Fortran only:
Substitute critical-section-trick
by `reduction(max:dphimax)` clause

Introduction to OpenMP [07]



OpenMP Exercise: Heat - Solution (1)

Location: `~/OpenMP/solution/heat`

- `heat.[F|c]` Original program
- `heat_x.[F|c]` Better serial program with interchanged nested loops
- `heatc.[F|c]` Extremely slow solution with `critical` section inside iteration loop
- `heatc2.[F|c]` Slow solution with `critical` section outside inner loop, one parallel region inside time step iteration loop (`it=...`)
- `heatc2_x.[F|c]` Fast solution with `critical` section outside inner loop, one parallel region inside iteration loop, interchanged nested loops
- `heatc3_x.[F|c]` ... and parallel region outside of `it=...` loop
- `heatc4_x.[F|c]` ... and abort criterion only each 20th iteration
- `heats2_x.F` Solution with `schedule(runtime)` clause
- `heatr2_x.F` Solution with `reduction` clause, one parallel region inside iteration loop [`reduction(max:...)` not available in C]

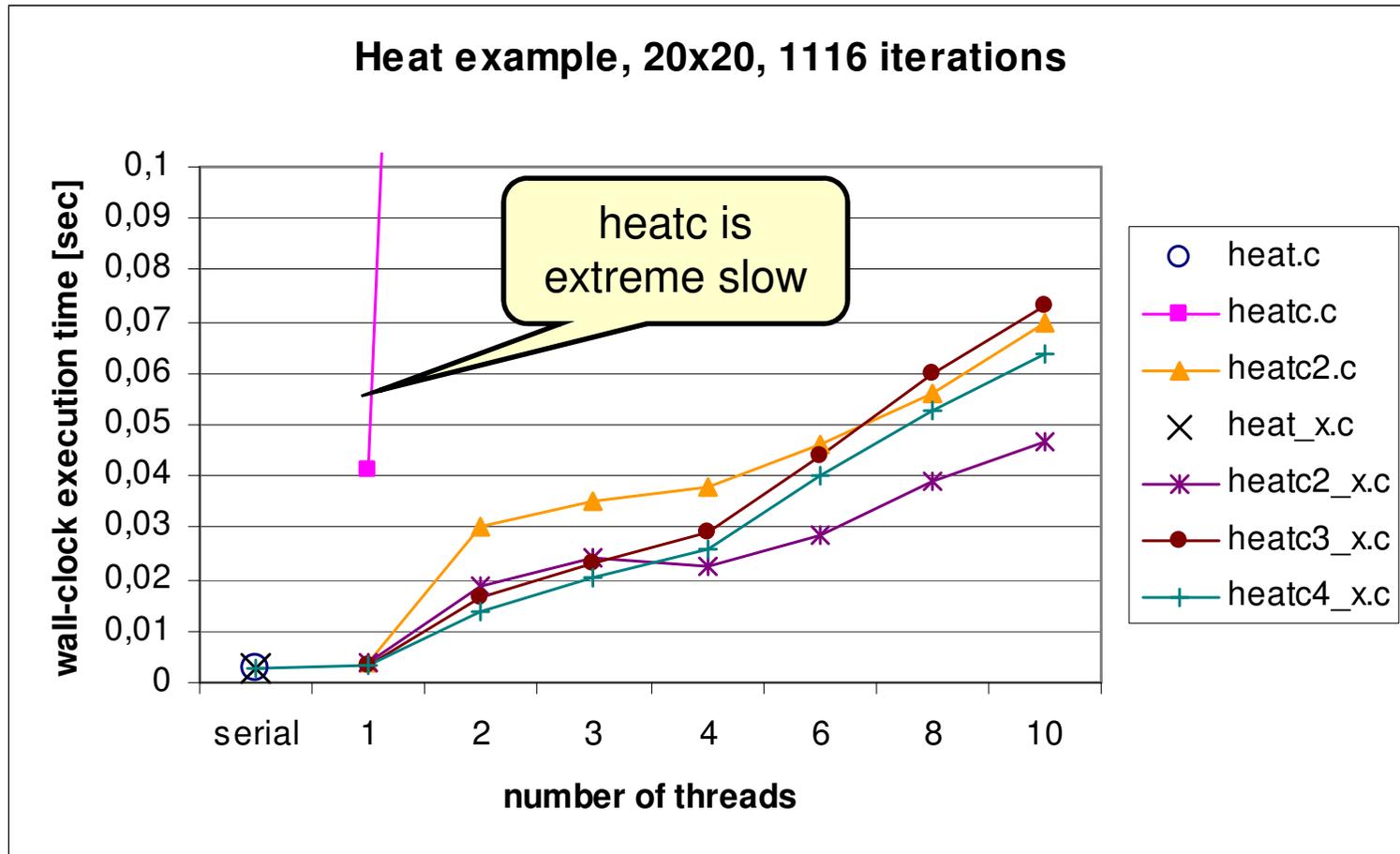


OpenMP Exercise: Heat - Solution (2)

- `heatc2` → `heatc2_x`
Loss of optimization with OpenMP directives (and compilers)
- For controlling the parallelization:
 - Version `20x20`: 1116 iterations
 - Version `80x80`: 14320 iterations
 - Version `250x250`: 15001 iterations [if `itmax = 15000` (default)]
110996 iterations [if `itmax` is extended to 150000]
- `heatc2_x` ↔ `heatc3_x`
Additional overhead for barriers and single sections
(including implied barrier)
must be compared with fork-join-overhead



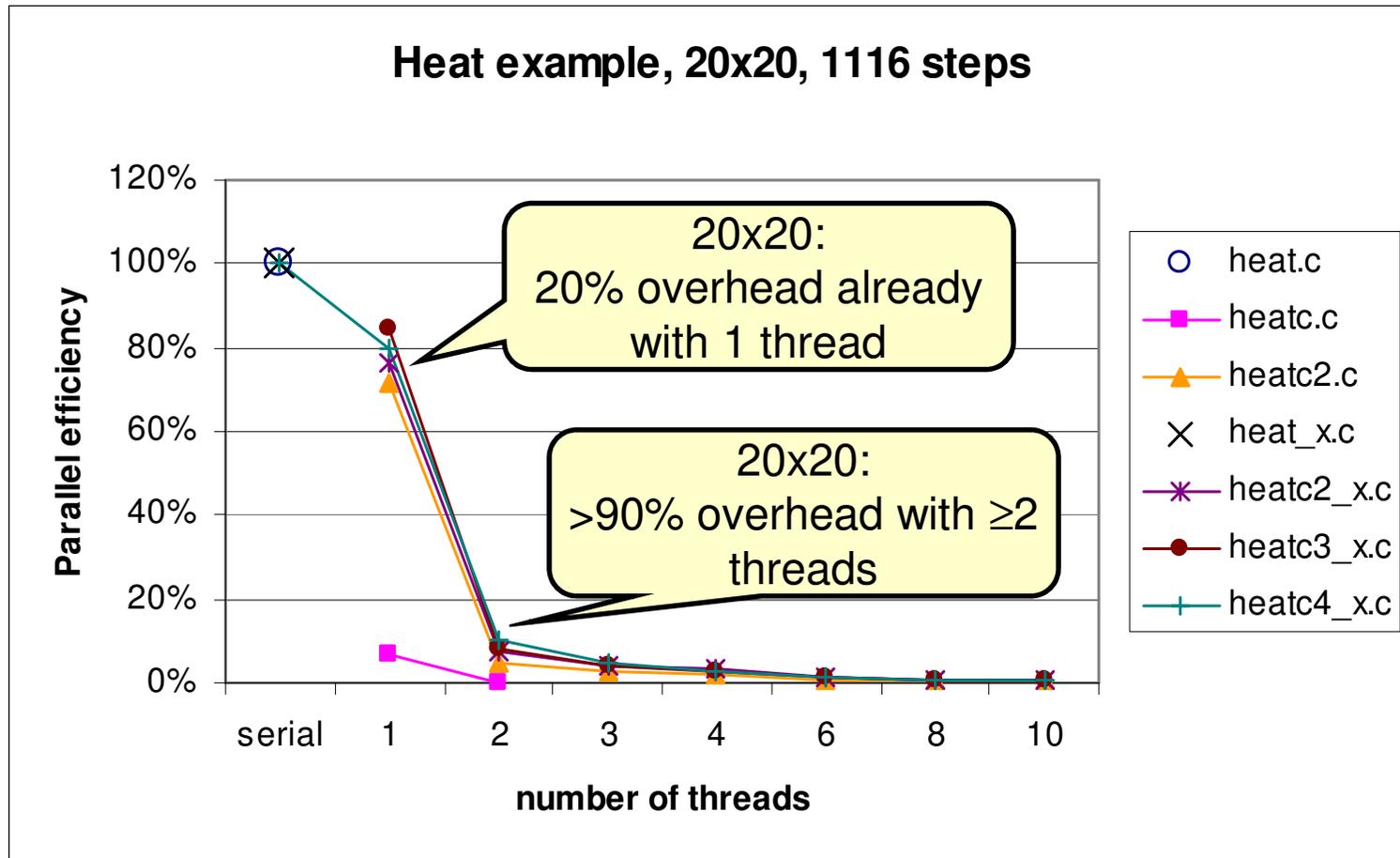
OpenMP Exercise: Heat - Solution (3) – 20x20 Time



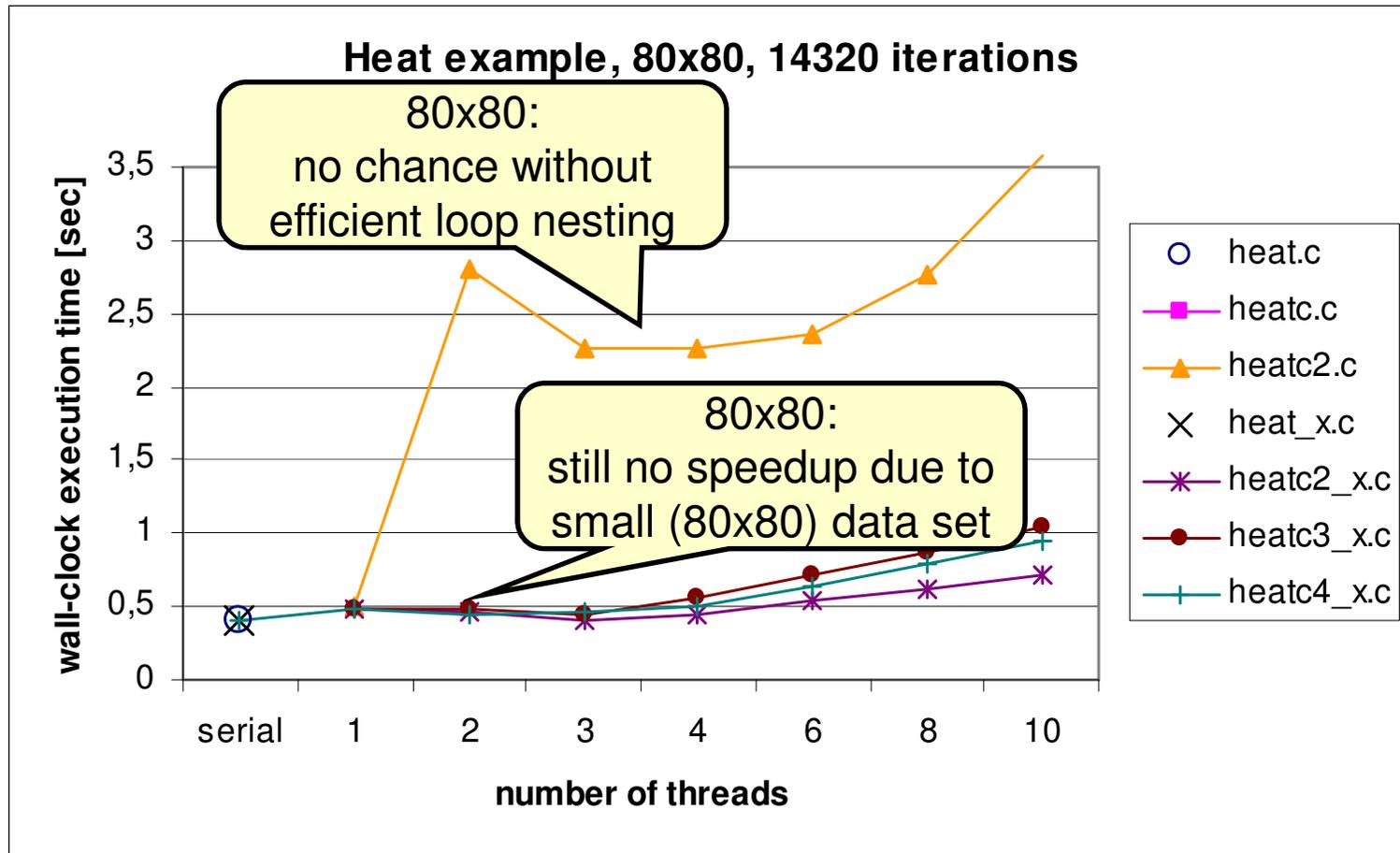
Measurements on NEC TX-7 (asama.hww.de), 16 CPUs, May 4-5, 2006



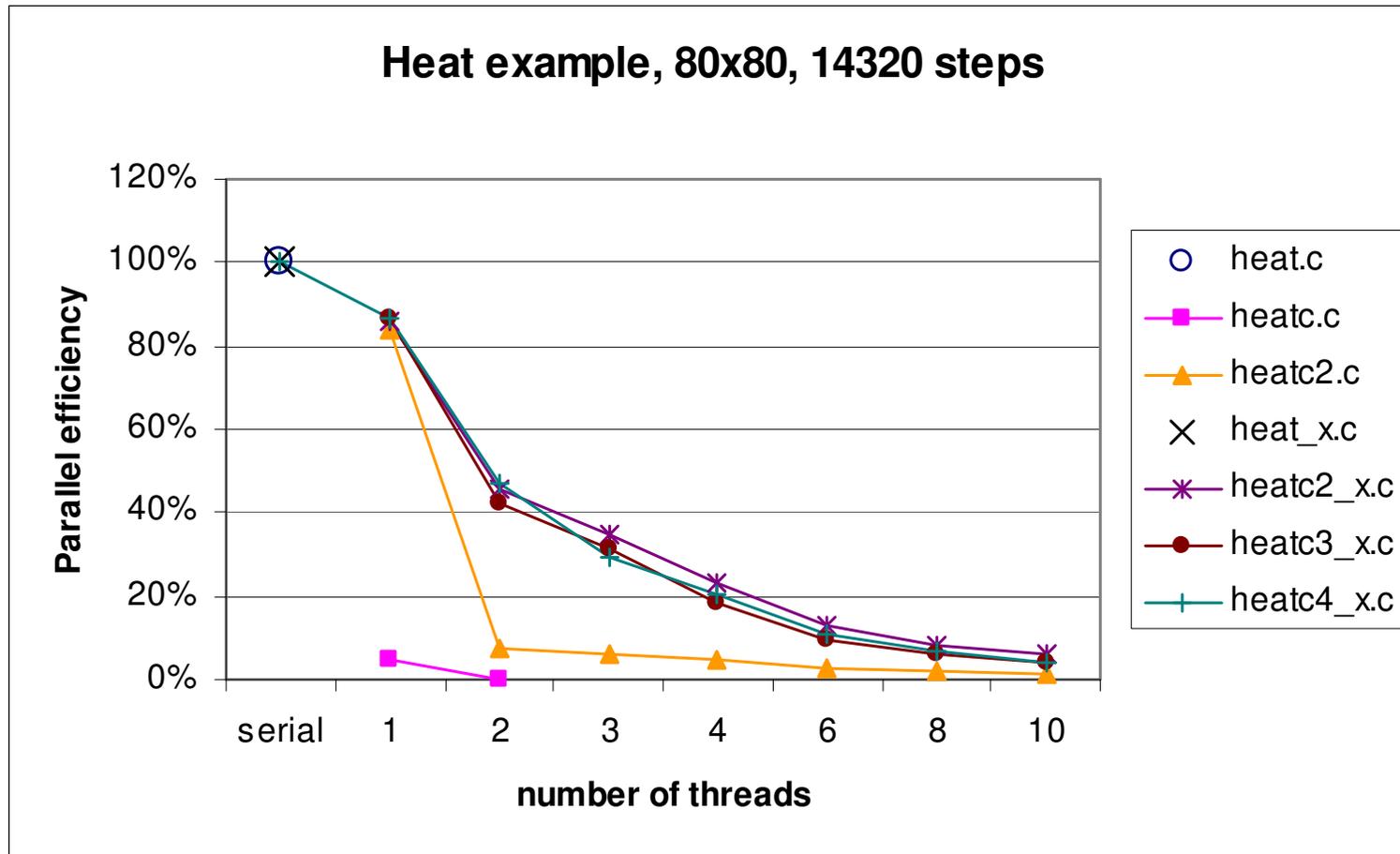
OpenMP Exercise: Heat - Solution (4) – 20x20 Efficiency



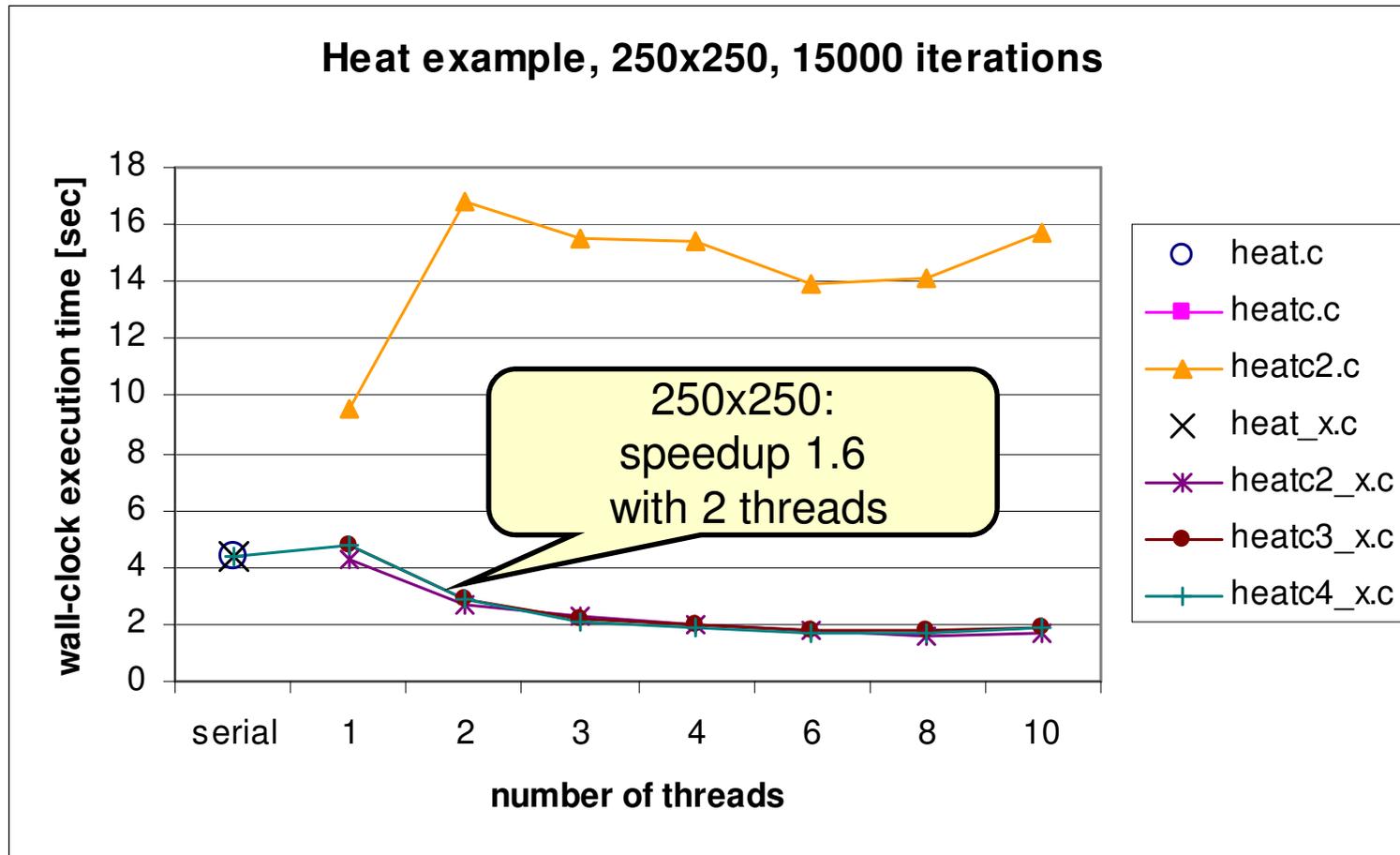
OpenMP Exercise: Heat - Solution (5) – 80x80 Time



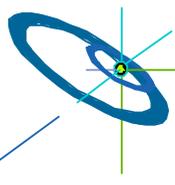
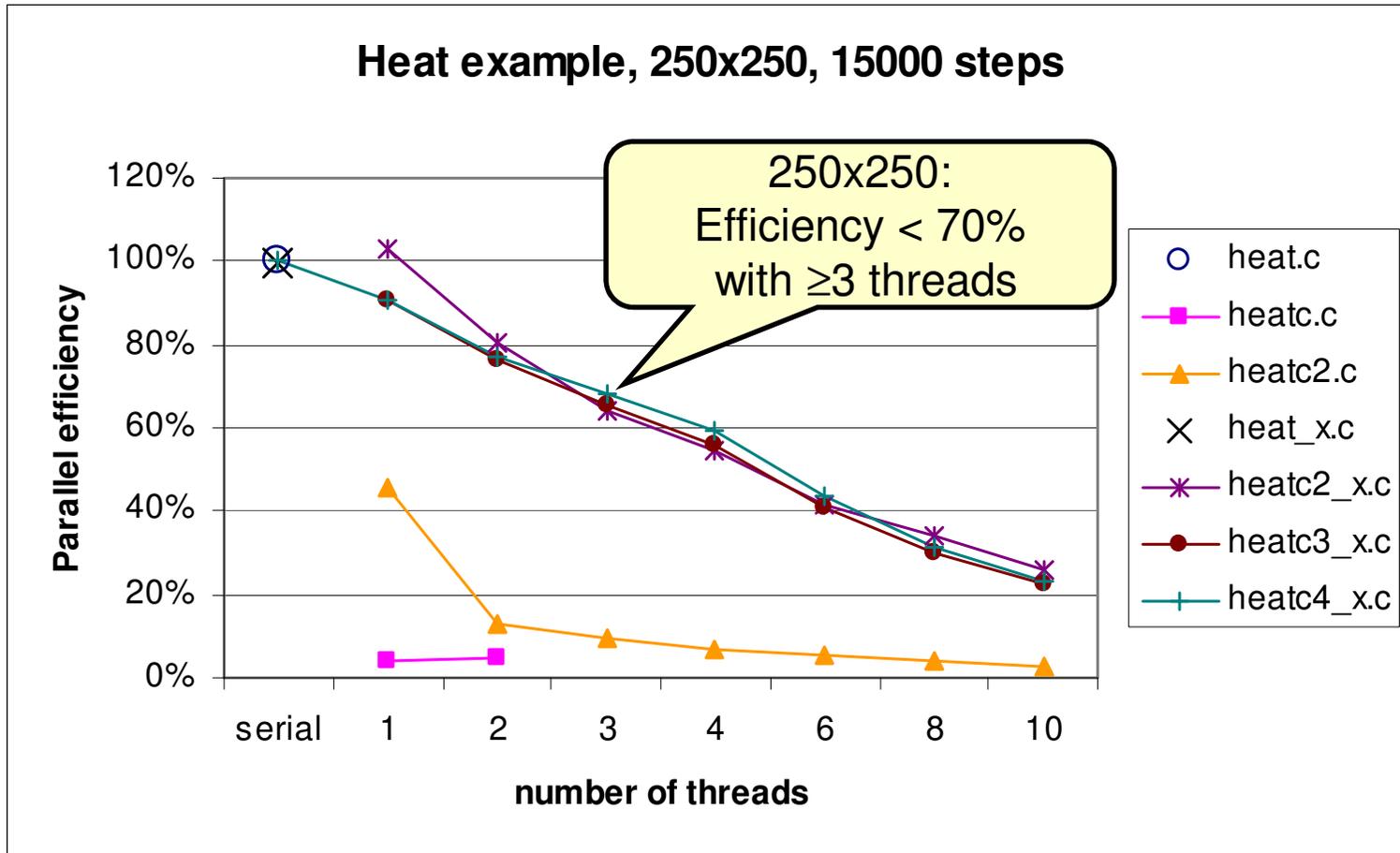
OpenMP Exercise: Heat - Solution (6) – 80x80 Efficiency



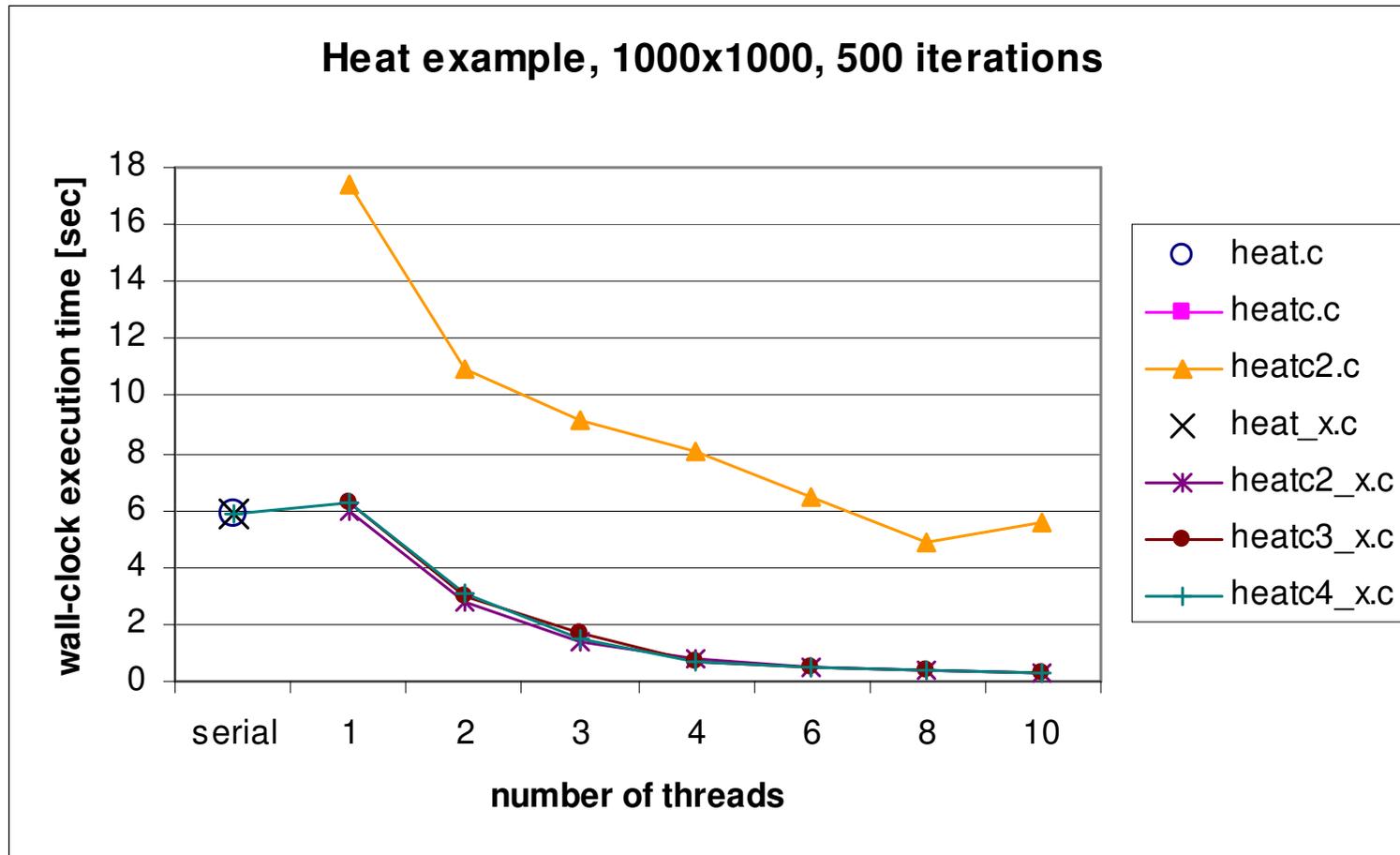
OpenMP Exercise: Heat - Solution (7) – 250x250 Time



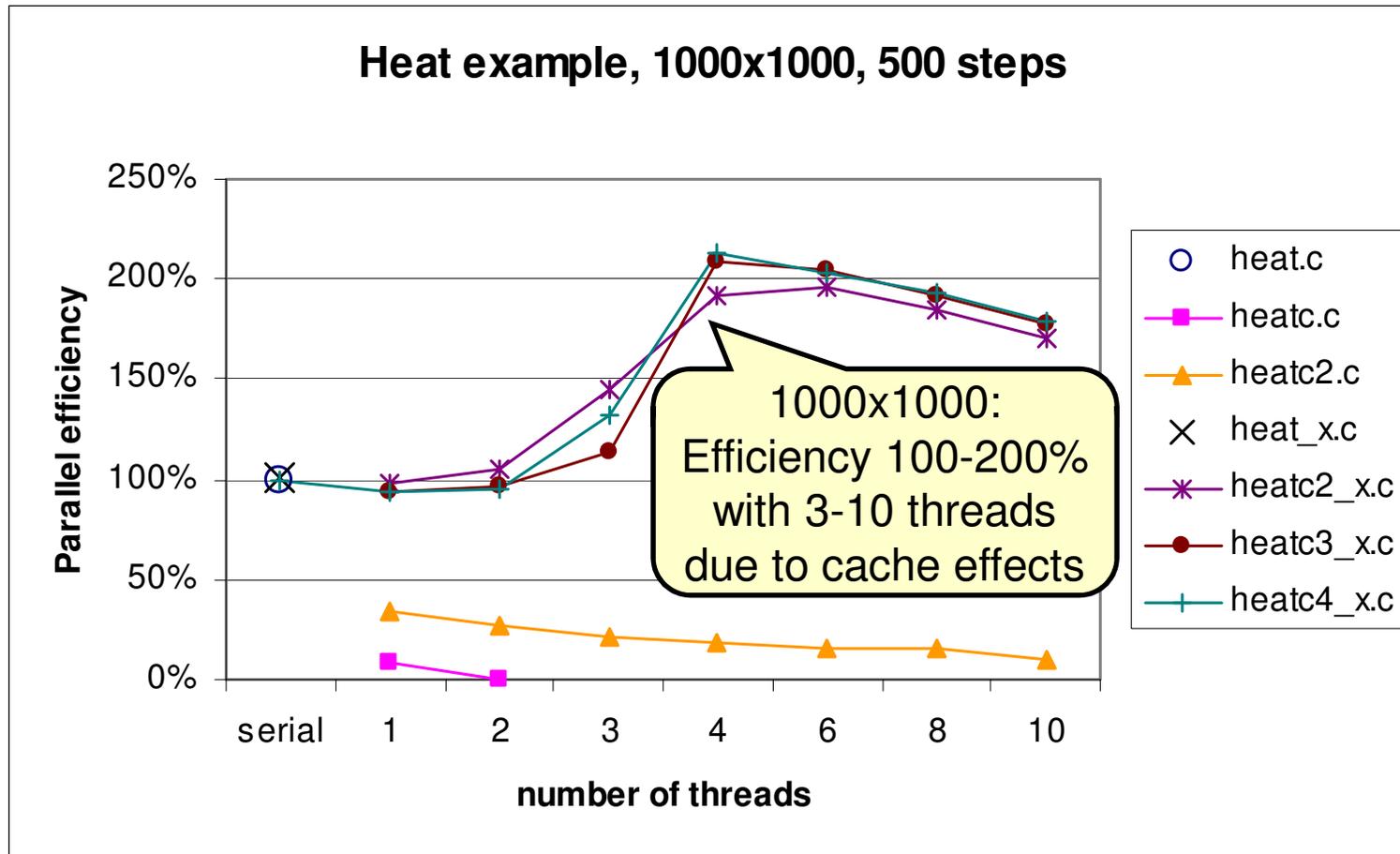
OpenMP Exercise: Heat - Solution (8) – 250x250 Efficiency



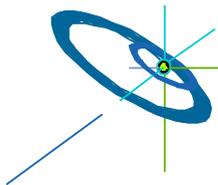
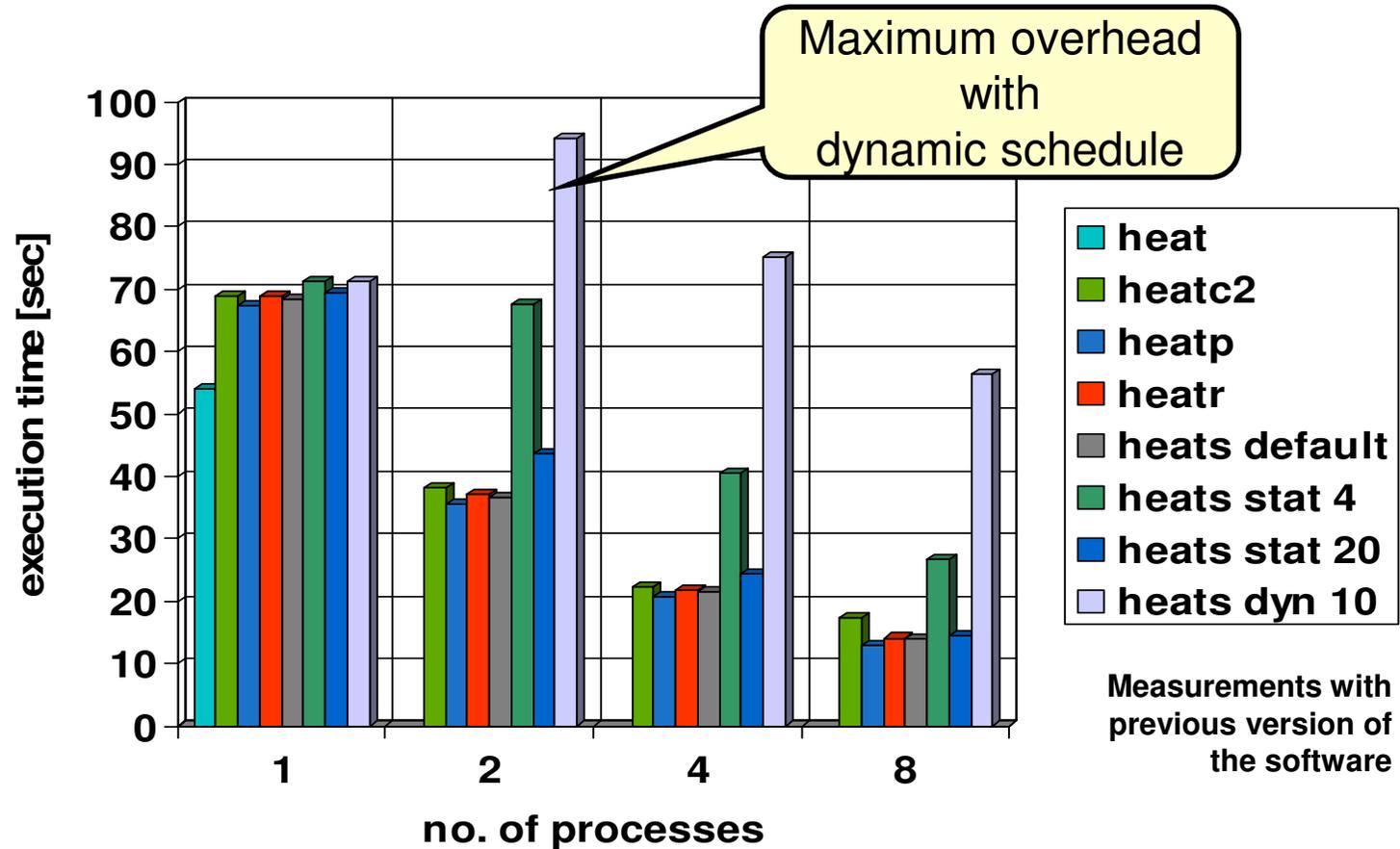
OpenMP Exercise: Heat - Solution (9) – 1000x1000 Time



OpenMP Exercise: Heat - Solution (10) – 1000x1000 Efficiency

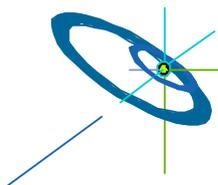


OpenMP Exercise: Heat - Execution Times F90 with 150x150



OpenMP Exercise: Heat Conduction - Summary

- Overhead for parallel versions using 1 thread.
- Be careful with compiler based optimizations.
- Datasets must be large enough to achieve good speed-up.
- Thread Checker should be used to guarantee zero race conditions.
- Be careful when using other than default scheduling strategies:
 - `dynamic` is generally expensive
 - `static`: overhead for small chunk sizes is clearly visible

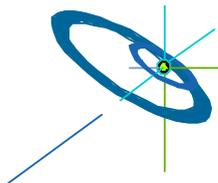


Outline — Summary of the OpenMP API

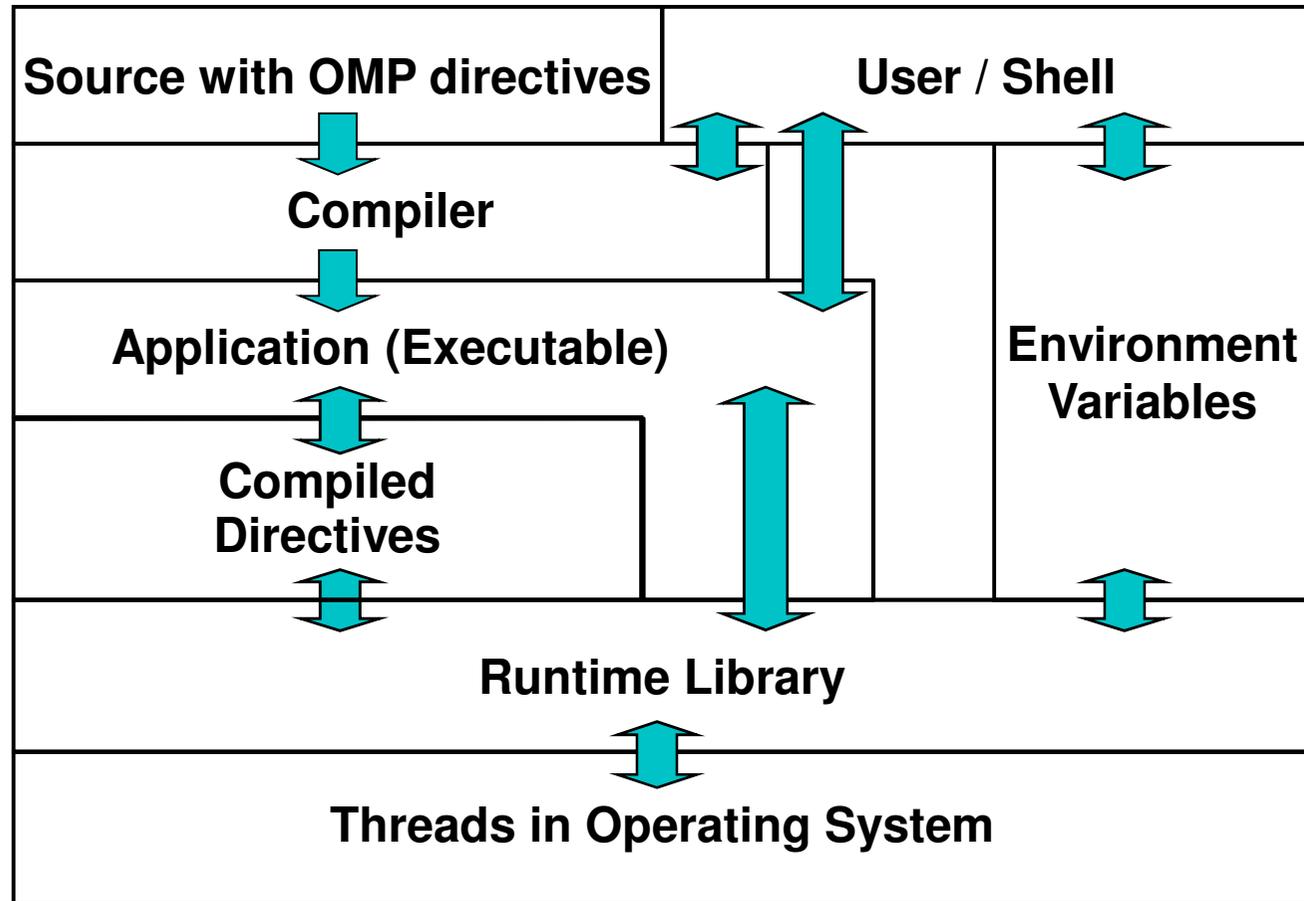
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 - Exercise 4: Heat
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- **OpenMP Pitfalls**

OpenMP Components

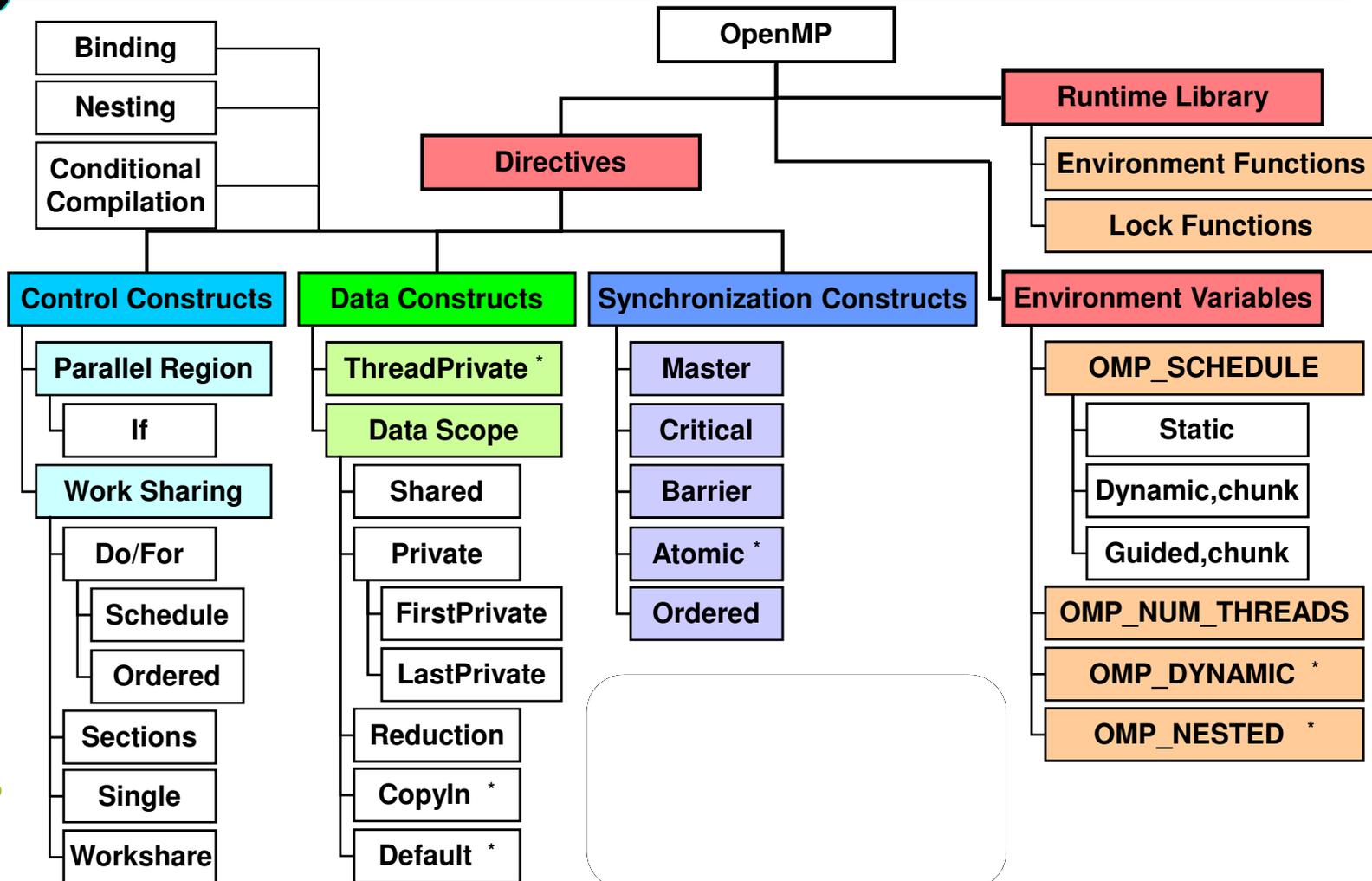
- Set of compiler directives
 - Control Constructs
 - **Parallel Regions**
 - **Worksharing constructs**
 - Data environment
 - Synchronization
- Runtime library functions
- Environment variables



OpenMP Architecture



OpenMP Constructs



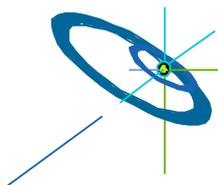
Outline — OpenMP Pitfalls

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Implementation-defined behavior

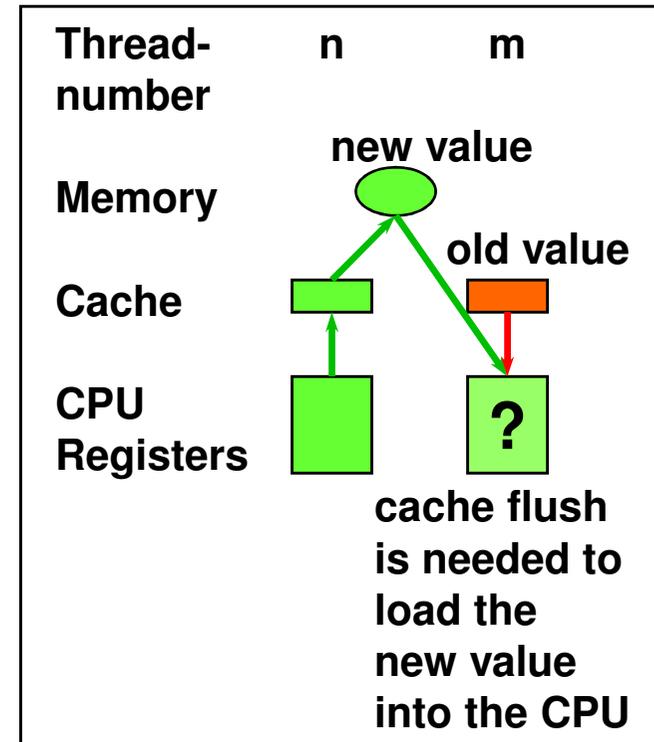
See Appendix D of the OpenMP 4.0 standard, e.g.:

- The size of the first chunk in SCHEDULE(GUIDED)
- default schedule for SCHEDULE(RUNTIME)
- default schedule
- default number of threads
- default for dynamic thread adjustment
- number of levels of nested parallelism supported
- atomic directives might be replaced by critical regions
- behavior in case of thread exhaustion
- allocation status of allocatable arrays that are not affected by COPYIN clause are undefined if dynamic thread mechanism is enabled
- Fortran: Is `include 'omp_lib.h'` or `use omp_lib` or both available?



Implied flush directive

- A FLUSH directive identifies a sequence point at which a consistent view of the shared memory is guaranteed
- It is implied at the following constructs:
 - BARRIER
 - CRITICAL and END CRITICAL
 - END {DO, FOR, SECTIONS}
 - END {SINGLE, WORKSHARE}
 - ORDERED AND END ORDERED
 - PARALLEL and END PARALLEL with their combined variants
 - Immediately before and after every task scheduling point (OpenMP ≥ 3.0)
- It is NOT implied at the following constructs:
 - Begin of DO, FOR, WORKSHARE, SECTIONS
 - **Begin of MASTER and END MASTER**
 - Begin of SINGLE
- Recommendation: Do **not** loop with testing on data modifications caused by other threads (without correct and sufficient flushing)
More secure: Use OpenMP synchronization methods



Two types of SMP errors

- Race Conditions
 - Data-Race: *Two threads access the same shared variable **and** at least one thread modifies the variable **and** the accesses are concurrent, i.e. unsynchronized*
 - The outcome of a program depends on the detailed timing of the threads in the team.
 - This is often caused by unintended share of data
- Deadlock
 - Threads lock up waiting on a locked resource that will never become free.
 - **Avoid lock functions if possible**
 - **At least avoid nesting different locks**



Example for race condition (1)

```
!$OMP PARALLEL SECTIONS
    A = B + C
!$OMP SECTION
    B = A + C
!$OMP SECTION
    C = B + A
!$OMP END PARALLEL SECTIONS
```

- The result varies unpredictably based on specific order of execution for each section.
- Wrong answers produced without warning!



Example for race condition (2)

```
!$OMP PARALLEL SHARED (X) , PRIVATE (TMP)
      ID = OMP_GET_THREAD_NUM()
!$OMP DO REDUCTION (+:X)
      DO 100 I=1,100
          TMP = WORK1(I)
          X = X + TMP
100 CONTINUE
!$OMP END DO NOWAIT
      Y(ID) = WORK2(X, ID)
!$OMP END PARALLEL
```

- The result varies unpredictably because the value of X isn't dependable until the barrier at the end of the do loop.
- Solution: Be careful when you use **NOWAIT**.



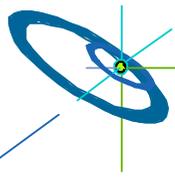
OpenMP programming recommendations

- Write SMP code that is
 - portable and
 - equivalent to the sequential form.
- Use tools like “Intel® Thread Checker” (formerly Assure).



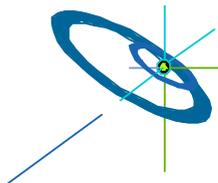
Sequential Equivalence

- Two forms of sequential equivalence
 - Strong SE: bitwise identical results.
 - Weak SE: equivalent mathematically but due to quirks of floating point arithmetic, not bitwise identical.
- Using a limited subset of OpenMP
e.g., no locks
- Advantages:
 - program can be tested, debugged and used in sequential mode
 - this style of programming is also less error prone



Rules for Strong Sequential Equivalence

- Control data scope with the base language
 - Avoid the data scope clauses.
 - Only use private for scratch variables local to a block (eg. temporaries or loop control variables) whose global initialization don't matter.
- Locate all cases where a shared variable can be written by multiple threads.
 - The access to the variable must be protected.
 - If multiple threads combine results into a single value, enforce sequential order.
 - Do not use the reduction clause carelessly.
(no floating point operations +, -, *)
 - **Use the ordered directive and the ordered clause.**
- Concentrate on loop parallelism/data parallelism



Example for Ordered Clause: pio.c / .f / .f90

```
#pragma omp for ordered
for (i=1;i<=n;i++)
{
  x=w*((double)i-0.5);
  myf=f(x);    /* f(x) should be expensive! */
}
#pragma omp ordered
{
  sum=sum+myf;
}
}
```

ordered clause

ordered directive

- “ordered” corresponds to “critical” + “order of execution”
- only efficient if workload outside ordered directive is large enough



Reproducible & efficient reduction results if OMP_NUM_THREADS is fixed

- On any platform with same rounding algorithm (e.g., IEEE)
- But with different OpenMP implementations and defaults
- Tricks:
 - Loop schedule(static, with fixed chunk size)
 - Reduction operation explicitly sequential
 - Disable dynamic adjustment of number of threads



Reproducible & efficient reduction results if OMP_NUM_THREADS is fixed

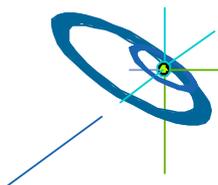
pio2.c

```
n=100000000; w=1.0/n; sum=0.0;
omp_set_dynamic(0);
#pragma omp parallel private (x,sum0,num_threads)
    shared(w,sum)
{
#ifdef _OPENMP
    num_threads=omp_get_num_threads();
#else
    num_threads=1
#endif
    sum0=sum;
#pragma omp for schedule(static, (n-1)/num_threads+1)
    for (i=1;i<=n;i++)
    { x=w*((double)i-0.5);
      sum0=sum0+4.0/(1.0+x*x);
    }
#pragma omp for ordered schedule(static,1)
    for (i=0;i<num_threads;i++)
    {
#pragma omp ordered
        sum=sum+sum0;
    }
}
pi=w*sum;
```

**Drawback: Thread Checker
returns always 2!
→ Wrong result!
See [8a] – talk on Intel®
Thread Checker – Example 7**

Rules for weak sequential equivalence

- For weak sequential equivalence only mathematically valid constraints are enforced.
 - **Floating point arithmetic is not associative and not commutative.**
 - **In many cases, no particular grouping of floating point operations is mathematically preferred so why take a performance hit by forcing the sequential order?**
 - In most cases, if you need a particular grouping of floating point operations, you have a bad algorithm.
- How do you write a program that is portable and satisfies weak sequential equivalence?
 - Follow the same rules as the strong case, but relax sequential ordering constraints.



Reentrant (= thread-safe) library functions

- Library functions (if called inside of parallel regions) must be reentrant
- **Automatically switched** if OpenMP option is used:
 - e.g., Intel compiler:
 - `efc -openmp -o my_prog my_prog.f or my_prog.f90` (Fortran)
 - `ecc -openmp -o my_prog my_prog.c` (C, C++)
- **Manually by compiler option:**
 - e.g., IBM compiler:
 - `xlf_r -O -qsmp=omp -o my_prog my_prog.f` (Fortran, fixed form)
 - `xlf90_r -O -qsmp=omp -o my_prog my_prog90.f` (Fortran, free form)
 - `xlC_r -O -qsmp=omp -o my_prog my_prog.c` (C)
 - The “_r” forces usage of reentrant library functions
- **Manually by programmer:** Some library function are using an internal buffer to store its state – one must use its reentrant counterpart:
 - e.g., reentrant `erand48()` instead of `drand48()`
`gmtime_r()` `gmtime()`
... ..

Optimization Problems – Overview

- Prevent unnecessary fork and join of parallel regions
 - if you can execute several loop / workshare / sections / single inside of one parallel region
- Prevent unnecessary synchronizations
 - e.g. with critical or ordered regions inside of loops
- Prevent false-sharing (of cache-lines)
- Prevent unnecessary cache-coherence or memory communication
 - E.g., same schedules for same memory access patterns
 - First touch on (cc)NUMA architectures
 - **To locate arrays/objects already in a parallelized initialization to the threads where they are mainly used**
 - Pin the threads to CPUs [not useful in time sharing on over-committed systems]
 - **Otherwise, after each time slice, threads may run on other CPUs**
 - **numactl, or LIKWID (portable !!!)**
 - `dplace -x2` (SGI), `O(1)` scheduler (HP), `SUNW_OMP_PROBIND` envir. (Sun)
 - `fplace -ro 1,2` *command* (Intel), ...
 - Do not pin management threads



Get a feeling for the involved overheads

Operation	Minimum overhead (cycles)	Scalability
Hit L1 cache	1-10	Constant
Function call	10-20	Constant
Thread ID	10-50	Constant, log, linear
Integer divide	50-100	Constant
Static do/for, no barrier	100-200	Constant
Miss all caches	100-300	Constant
Lock acquisition	100-300	Depends on contention
Dynamic do/for, no barrier	1000-2000	Depends on contention
Barrier	200-500	Log, linear
Parallel	500-1000	Linear
Ordered	5000-10000	Depends on contention

All numbers are approximate!! They are very platform dependent !!



Optimization Problems

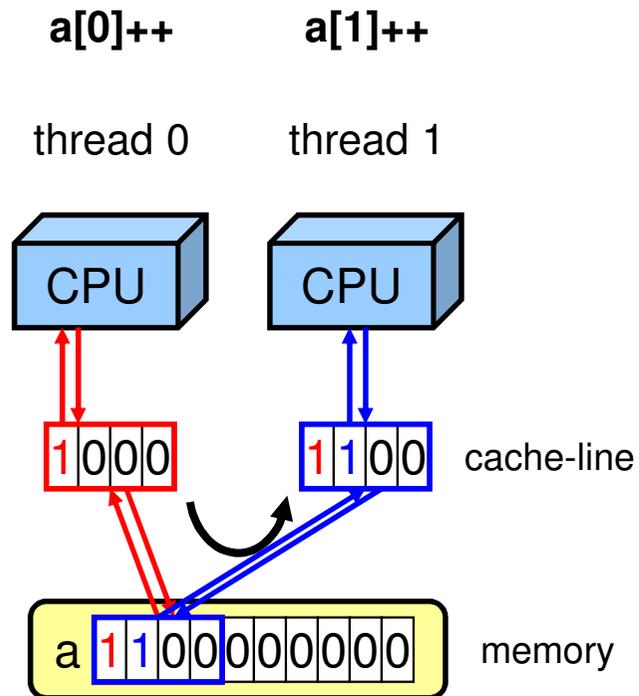
- Prevent frequent synchronizations, e.g., with critical regions

```
max = 0;
#pragma omp parallel private(partial_max)
{
    partial_max = 0;
#pragma omp for
    for (i=0; i<10000; i++)
    {
        x[i] = ...;
        if (x[i] > partial_max) partial_max = x[i];
    }
#pragma omp critical
    if (partial_max > max) max = partial_max;
}
```

- Loop: `partial_max` is updated locally up to `10000/#threads` times
- Critical region: `max` is updated only up to `#threads` times



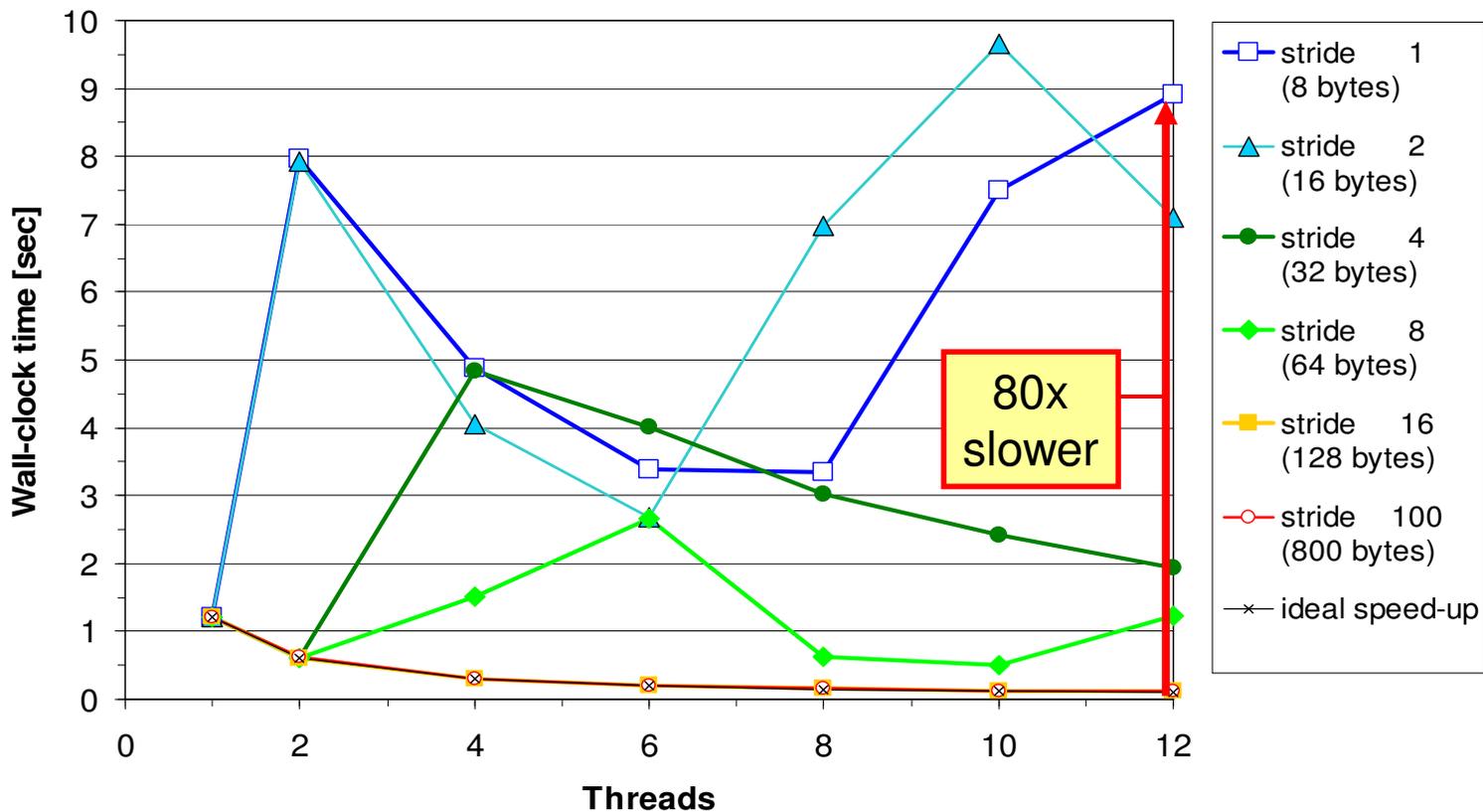
False-sharing



- Several threads are accessing data through the same cache-line.
- This cache-line has to be moved between these threads.
- This is very time-consuming. ■



False-sharing – results from the experiment



Although each thread accesses **independent variables**, the performance will be terrible, if these variables are located in the same cache-line

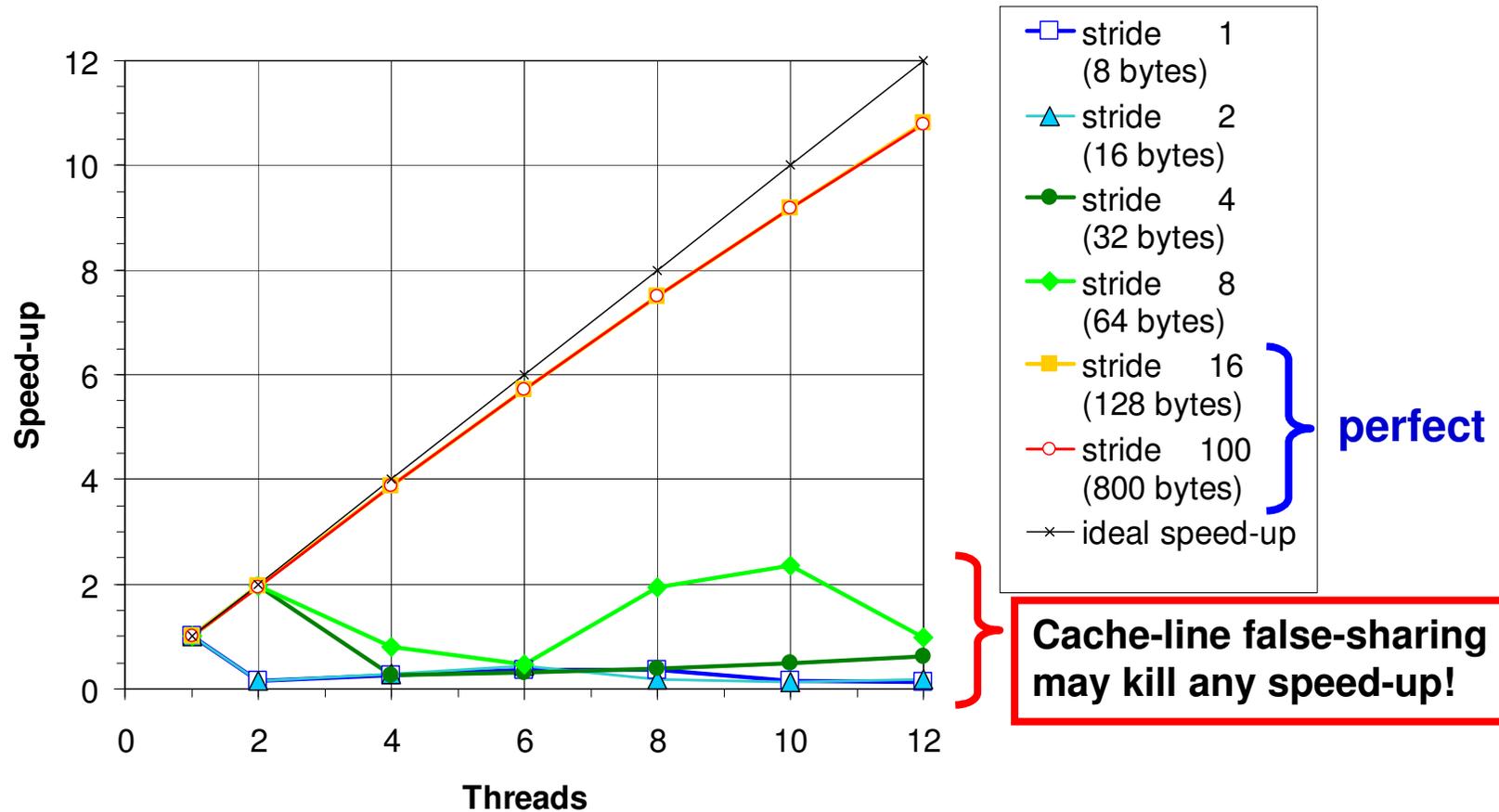
OpenMP Rolf Rabenseifner
 [7] Slide 134 /139 Höchstleistungsrechenzentrum Stuttgart

H L R I S

Measurements on NEC TX-7 with **128 bytes cache lines**,
 timings with false-sharing (stride 1-8 with more than 1 thread) were varying from run to run.

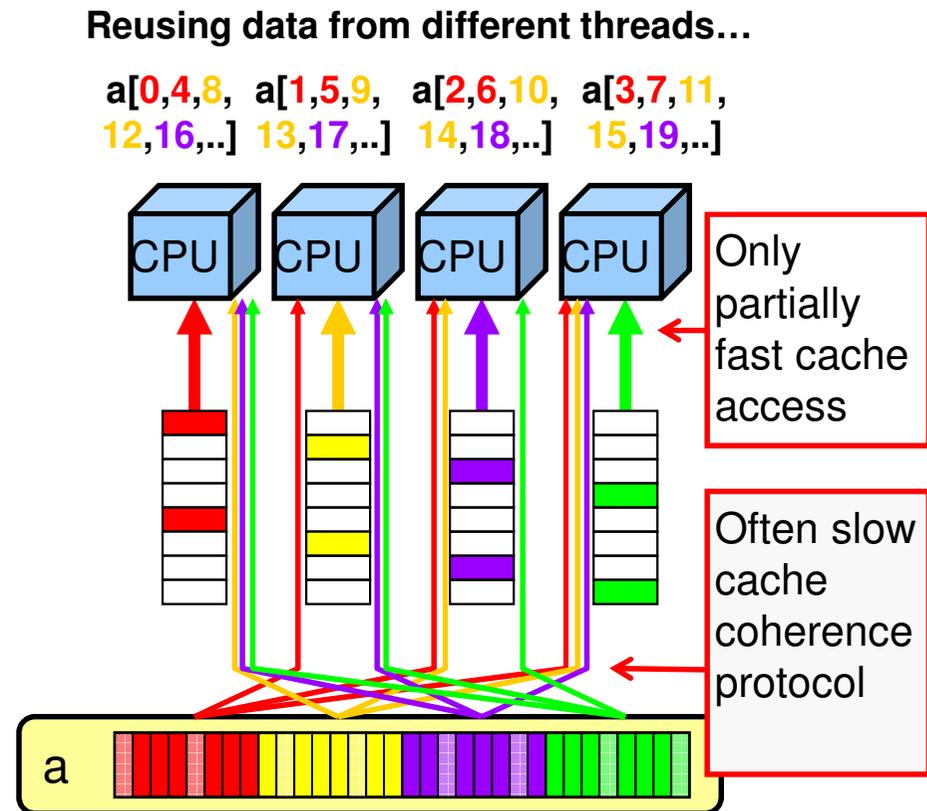
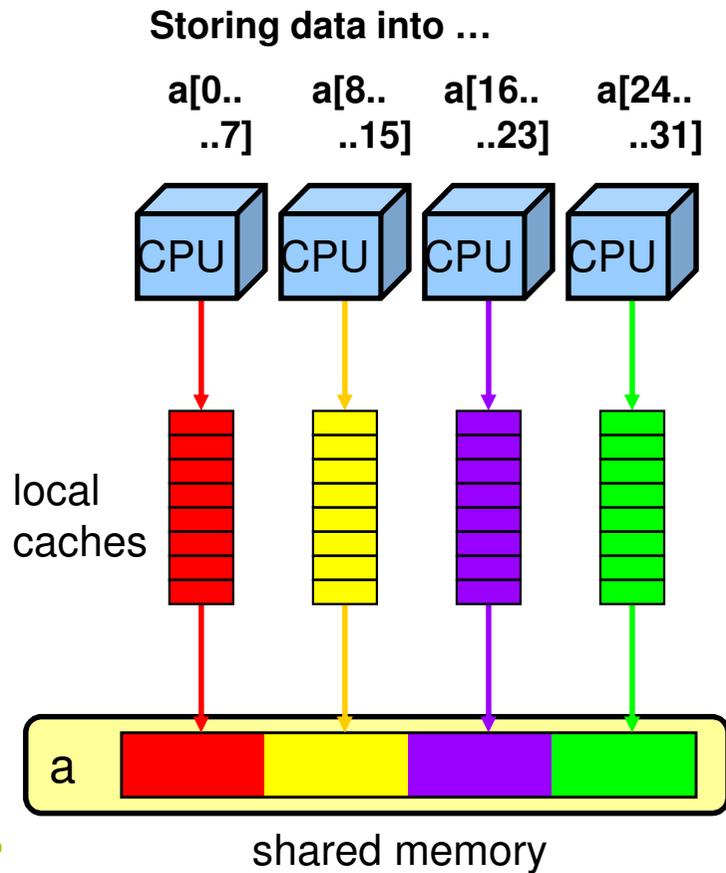
Test program, see
 Appendix: piarr.c

False-sharing – same with speed-up



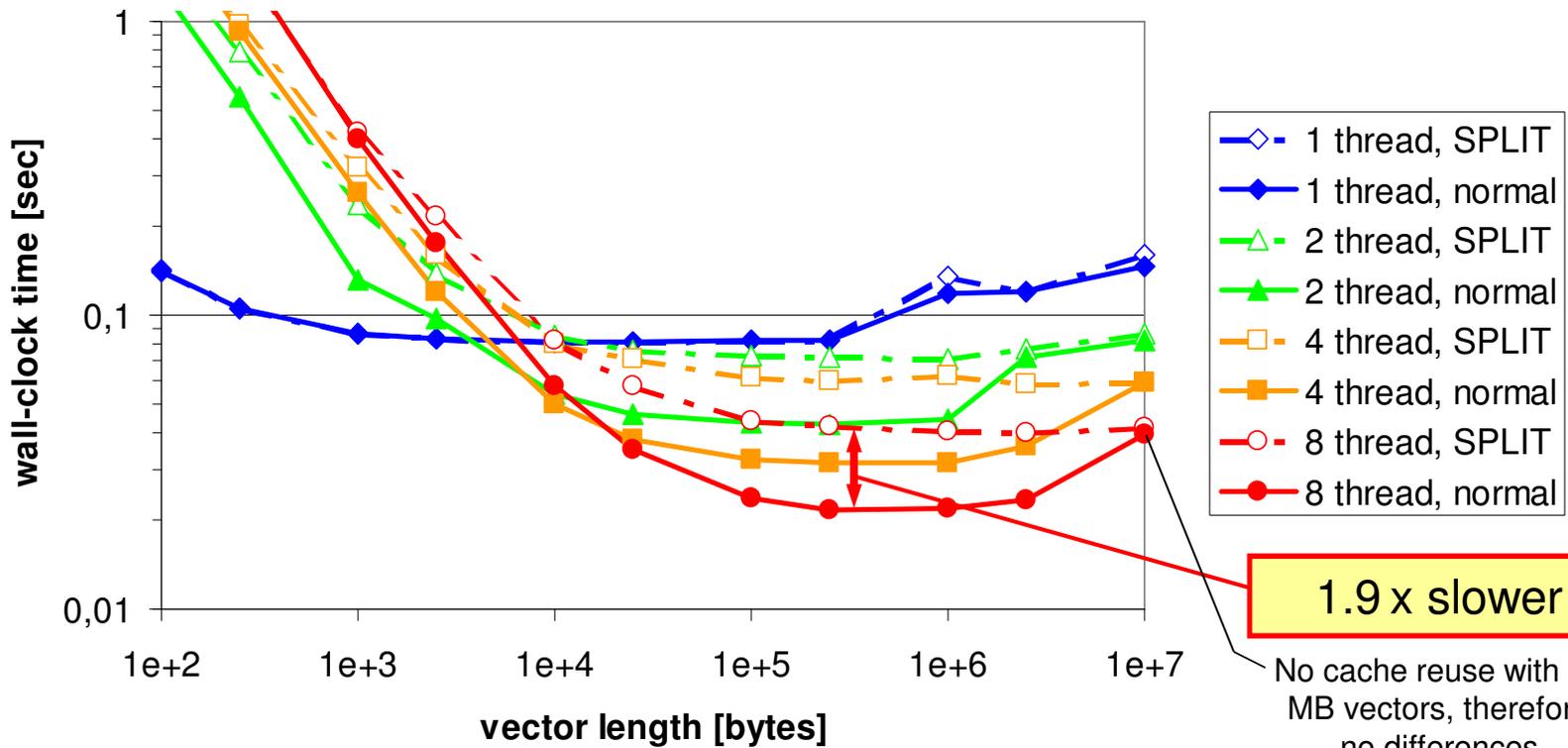
Measurements on NEC TX-7 with **128 bytes cache lines**, timings with false-sharing (stride 1-8 with more than 1 thread) were varying from run to run.

Communication overhead, e.g., due to different schedules



Communication overhead – results from the experiment

Calculation of pi with vector chunks
Wall-clock time - **the smaller the better!**
Timing on NEC TX-7, with n=10,000,000



1.9 x slower

No cache reuse with 10 MB vectors, therefore no differences

Significant performance penalties

because several threads are accessing **the same data** in different loops

Test program, see Appendix: pivec.c

Acknowledgements

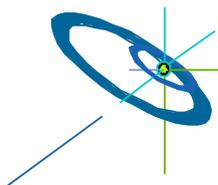
Thanks to

- Rainer Keller (Hochschule für Technik, Stuttgart)
- Matthias Müller (RWTH Aachen)
- Isabel Loebich



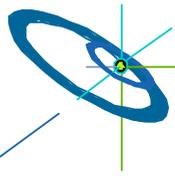
OpenMP Summary

- Standardized compiler directives for shared memory programming
- Fork-join model based on threads
- Support from all relevant hardware vendors
- OpenMP offers an incremental approach to parallelism
- OpenMP allows to keep one source code version for scalar and parallel execution
- Equivalence to sequential program is possible if necessary
 - strong equivalence
 - weak equivalence
 - no equivalence
- OpenMP programming includes race conditions and deadlocks, but a subset of OpenMP can be considered safe
- Tools like Intel® Thread Checker help to write correct parallel programs ■



Appendix

Introduction to OpenMP [07]



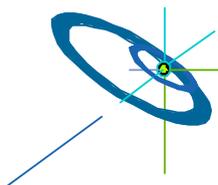
OpenMP
[7] Slide 140

Rolf Rabenseifner
Hochleistungsrechenzentrum Stuttgart



Appendix – Content

- Example pi, written in C
- Example pi, written in Fortran (fixed form)
- Example pi, written in Fortran (free form)
- Example heat
 - heatc2.c – parallel version in C, with critical region (4 pages)
 - heatr.f – parallel version in Fortran, with reduction clause (4 pages)
- Cache-line false-sharing experiment: piarr.c
- Communication overhead / different schedules experiment: pivec.c



Example pi, written in C

- pi.c – sequential code
- pi0.c – sequential code with a parallel region, verifying a team of threads
- pic2.c – parallel version with a critical region outside of the loop
- pir.c – parallel version with a reduction clause
- pir2.c – parallel version with combined `parallel for`
- pio.c – parallel version with ordered region
- pio2.c – parallel version with ordered execution if the number of threads is fixed



pi.c – sequential code

The include and timing blocks are removed on the next slides

```
#include <stdio.h>
#include <time.h>
#include <sys/time.h>
#ifdef _OPENMP
# include <omp.h>
#endif
#define f(A) (4.0/(1.0+A*A))
const int n = 10000000;
include block
```

```
int main(int argc, char** argv)
{
    int i;
    double w,x,sum,pi;
```

```
    clock_t t1,t2;
    struct timeval tv1,tv2;
    struct timezone tz;
# ifdef _OPENMP
    double wt1,wt2;
# endif
timing block A
```

```
    gettimeofday(&tv1, &tz);
# ifdef _OPENMP
    wt1=omp_get_wtime();
# endif
    t1=clock();
timing block B
```

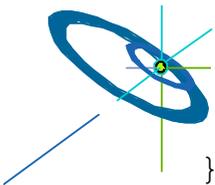
```
/* pi = integral [0..1] 4/(1+x**2) dx */
w=1.0/n;
sum=0.0;
for (i=1;i<=n;i++)
{
    x=w*((double)i-0.5);
    sum=sum+f(x);
}
pi=w*sum;
the calculation
```

```
    t2=clock();
timing block C
# ifdef _OPENMP
    wt2=omp_get_wtime();
# endif
    gettimeofday(&tv2, &tz);
    printf( "computed pi = %24.16g\n", pi);
    printf( "CPU time (clock)
    = %12.4g sec\n", (t2-t1)/1000000.0 );
# ifdef _OPENMP
    printf( "wall clock time
    (omp_get_wtime) = %12.4g sec\n",
    wt2-wt1 );
# endif
    printf( "wall clock time (gettimeofday)
    = %12.4g sec\n",
    (tv2.tv_sec-tv1.tv_sec) +
    (tv2.tv_usec-tv1.tv_usec)*1e-6 );

    return 0;
```

pi0.c – only verification of team of threads – without parallelization

```
--- INCLUDE BLOCK ---
#define f(A) (4.0/(1.0+A*A))
const int n = 10000000;
int main(int argc, char** argv)
{
    int i;
    double w,x,sum,pi;
    --- TIMING_BLOCK A ---
    # ifdef _OPENMP
        int myrank, num_threads;
    # pragma omp parallel private(myrank,num_threads)
        {
            myrank = omp_get_thread_num();
            num_threads = omp_get_num_threads();
            printf("I am thread %2d of %2d threads\n", myrank, num_threads);
        } /* end omp parallel */
    # else
        printf("This program is not compiled with OpenMP\n");
    # endif
    --- TIMING_BLOCK B ---
    /* calculate pi = integral [0..1] 4/(1+x**2) dx */
    w=1.0/n;
    sum=0.0;
    for (i=1;i<=n;i++)
    {
        x=w*((double)i-0.5);
        sum=sum+f(x);
    }
    pi=w*sum;
    --- TIMING_BLOCK C ---
    return 0;
}
```



pic2.c

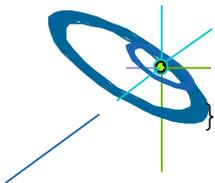
parallelization with critical region outside of the loop

```
--- INCLUDE BLOCK ---
#define f(A) (4.0/(1.0+A*A))
const int n = 10000000;
int main(int argc, char** argv)
{
    int i;
    double w, x, sum, sum0, pi;
    --- TIMING BLOCK A ---
    --- PRINT NUM_THREADS ---
    --- TIMING BLOCK B ---
    /* pi = integral [0..1] 4/(1+x**2) dx */
    w=1.0/n;
    sum=0.0;
    #pragma omp parallel private(x, sum0), shared(w, sum)
    {
        sum0=0.0;
        # pragma omp for
        for (i=1; i<=n; i++)
        {
            x=w*((double)i-0.5);
            sum0=sum0+f(x);
        }
        # pragma omp critical
        {
            sum=sum+sum0;
        }
    } /*end omp parallel*/
    pi=w*sum;
    --- TIMING BLOCK C ---
    return 0;
}
```

```
# ifdef _OPENMP
#   pragma omp parallel
#   {
#       pragma omp single
#       printf("OpenMP-parallel with %ld
#           threads\n", omp_get_num_threads());
#   } /* end omp parallel */
# endif
```

←

shortened according to advanced practical 2



pir.c – parallelization with reduction clause

```
--- INCLUDE BLOCK ---
#define f(A) (4.0/(1.0+A*A))
const int n = 10000000;
int main(int argc, char** argv)
{
    int i;
    double w,x,sum,pi;
    --- TIMING BLOCK A ---
    --- PRINT NUM_THREADS ---
    --- TIMING BLOCK B ---
    /* calculate pi = integral [0..1] 4/(1+x**2) dx */
    w=1.0/n;
    sum=0.0;
    #pragma omp parallel private(x), shared(w,sum)
    {
    # pragma omp for reduction(+:sum)
        for (i=1;i<=n;i++)
        {
            x=w*((double)i-0.5);
            sum=sum+f(x);
        }
    } /*end omp parallel*/
    pi=w*sum;

    --- TIMING BLOCK C ---
    return 0;
}
```

pir2.c – combined parallel for with reduction clause

```
--- INCLUDE BLOCK ---
#define f(A) (4.0/(1.0+A*A))
const int n = 10000000;
int main(int argc, char** argv)
{
    int i;
    double w,x,sum,pi;
    --- TIMING BLOCK A ---
    --- PRINT NUM_THREADS ---
    --- TIMING BLOCK B ---
    /* calculate pi = integral [0..1] 4/(1+x**2) dx */
    w=1.0/n;
    sum=0.0;
    #pragma omp parallel for private(x), shared(w), reduction(+:sum)
    for (i=1;i<=n;i++)
    {
        x=w*((double)i-0.5);
        sum=sum+f(x);
    }
    /*end omp parallel for*/
    pi=w*sum;

    --- TIMING BLOCK C ---
    return 0;
}
```



pio.c – parallelization with ordered clause

```
--- INCLUDE BLOCK ---
#define f(A) (4.0/(1.0+A*A))
const int n = 10000000;
int main(int argc, char** argv)
{
    int i;
    double w, x, sum, myf, pi;
    --- TIMING BLOCK A ---
    --- PRINT NUM_THREADS ---
    --- TIMING BLOCK B ---
    /* calculate pi = integral [0..1] 4/(1+x**2) dx */
    w=1.0/n;
    sum=0.0;
    #pragma omp parallel private(x,myf), shared(w, sum)
    {
        # pragma omp for ordered
        for (i=1;i<=n;i++)
        {
            x=w*((double)i-0.5);
            myf = f(x);
            # pragma omp ordered
            {
                sum=sum+myf;
            }
        }
    } /*end omp parallel*/
    pi=w*sum;
    --- TIMING BLOCK C ---
    return 0;
}
```

CAUTION
The sequentialization of the ordered region may cause heavy synchronization overhead



pio2.c – ordered, but only if number of threads is fixed

```
...
double w, x, sum, sum0, pi;
...
/* calculate pi = integral [0..1] 4/(1+x**2) dx */
w=1.0/n;
sum=0.0;
#pragma omp parallel private(x, sum0, num_threads), shared(w, sum)
{
    sum0=0.0;
#ifdef _OPENMP
    num_threads=omp_get_num_threads();
#else
    num_threads=1
#endif
#pragma omp for schedule(static, (n-1)/num_threads)
    for (i=1; i<=n; i++)
    {
        x=w*((double)i-0.5);
        sum0=sum0+f(x);
    }
#pragma omp for ordered schedule(static, (n-1)/num_threads)
    for (i=0; i<num_threads; i++)
    {
#pragma omp ordered
        sum=sum+sum0;
    }
} /*end omp parallel*/
pi=w*sum;
...
```

CAUTION

1. Only if the number of threads is fixed AND if the floating point rounding is the same, then the result is the same on two different platforms and any repetition of this program.
2. This program cannot be verified with Assure because it has to call `omp_get_num_threads()`.
3. To use Assure, the second loop must be substituted by the critical region as shown in `pic2.c`

Example pi, written in Fortran (fixed form)

- pi.f – sequential code
- pi0.f – sequential code with a parallel region, verifying a team of threads
- pic2.f – parallel version with a critical region outside of the loop
- pir.f – parallel version with a reduction clause
- pir2.f – parallel version with combined `parallel for`
- pio.f – parallel version with ordered region
- pio2.f – parallel version with ordered execution if the number of threads is fixed



pi.f – sequential code

The timing blocks are removed on the next slides

```
program compute_pi
  implicit none
  integer n,i
  double precision w,x,sum,pi,f,a
  parameter (n=10 000 000)

! times using cpu_time
  real t0
  real t1
!--unused-- include 'omp_lib.h'
!$ double precision omp_get_wtime
!$ double precision wt0,wt1
! function to integrate
  f(a)=4.d0/(1.d0+a*a)
!$ wt0=omp_get_wtime()
  call cpu_time(t0)
! calculate pi = integral [0..1] 4/(1+x**2) dx
  w=1.0d0/n
  sum=0.0d0
  do i=1,n
    x=w*(i-0.5d0)
    sum=sum+f(x)
  enddo
  pi=w*sum
  call cpu_time(t1)
!$ wt1=omp_get_wtime()
  write (*,'(/,a,1pg24.16)') 'computed pi = ', pi
  write (*,'(/,a,1pg12.4)') 'cpu_time : ', t1-t0
!$ write (*,'(/,a,1pg12.4)') 'omp_get_wtime:', wt1-wt0
end
```

timing block A

timing block B

the calculation

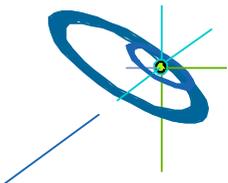
timing block C

S



pi0.f – only verification of team of threads – without parallelization

```
program compute_pi
implicit none
integer n,i
double precision w,x,sum,pi,f,a
parameter (n=10 000 000)
--- TIMING BLOCK A ---
!$ integer omp_get_thread_num, omp_get_num_threads
!$ integer myrank, num_threads
logical openmp_is_used
! function to integrate
f(a)=4.d0/(1.d0+a*a)
!$omp parallel private(myrank, num_threads)
!$ myrank = omp_get_thread_num()
!$ num_threads = omp_get_num_threads()
!$ write (*,*) 'I am thread',myrank, 'of',num_threads,'threads'
!$omp end parallel
openmp_is_used = .false.
!$ openmp_is_used = .true.
if (.not. openmp_is_used) then
write (*,*) 'This program is not compiled with OpenMP'
endif
--- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0d0/n
sum=0.0d0
do i=1,n
x=w*(i-0.5d0)
sum=sum+f(x)
enddo
pi=w*sum
--- TIMING BLOCK C ---
end
```



pic2.f

parallelization with critical region outside of the loop

```
program compute_pi
implicit none
integer n,i
double precision w,x,
+      sum, sum0, pi, f, a
parameter (n=10 000 000)
--- TIMING BLOCK A ---
! function to integrate
f(a)=4.d0/(1.d0+a*a)
--- PRINT NUM_THREADS
--- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0d0/n
sum=0.0d0
!$OMP PARALLEL PRIVATE(x, sum0), SHARED(w, sum)
sum0=0.0d0
!$OMP DO
do i=1,n
x=w*(i-0.5d0)
sum0=sum0+f(x)
enddo
!$OMP END DO
!$OMP CRITICAL
sum=sum+sum0
!$OMP END CRITICAL
!$OMP END PARALLEL
pi=w*sum
--- TIMING BLOCK C ---
end
```

```
!$ integer omp_get_num_threads
!$omp parallel
!$omp single
!$ write(*,*)'OpenMP-parallel with',
!$ + omp_get_num_threads(),'threads'
!$omp end single
!$omp end parallel
```

← shortened according to advanced practical 2

pir.f – parallelization with reduction clause

```
program compute_pi
  implicit none
  integer n,i
  double precision w,x,sum,pi,f,a
  parameter (n=10 000 000)
  --- TIMING BLOCK A ---
! function to integrate
  f(a)=4.d0/(1.d0+a*a)
  --- PRINT NUM_THREADS
  --- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
  w=1.0d0/n
  sum=0.0d0
!$OMP PARALLEL PRIVATE(x), SHARED(w, sum)
!$OMP DO REDUCTION(+:sum)
  do i=1,n
    x=w*(i-0.5d0)
    sum=sum+f(x)
  enddo
!$OMP END DO
!$OMP END PARALLEL
  pi=w*sum
  --- TIMING BLOCK C ---
end
```



pir2.f – combined parallel do with reduction clause

```
program compute_pi
  implicit none
  integer n,i
  double precision w,x,sum,pi,f,a
  parameter (n=10 000 000)
  --- TIMING BLOCK A ---
! function to integrate
  f(a)=4.d0/(1.d0+a*a)
  --- PRINT NUM_THREADS
  --- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
  w=1.0d0/n
  sum=0.0d0
!$OMP PARALLEL DO PRIVATE(x), SHARED(w), REDUCTION(+:sum)
  do i=1,n
    x=w*(i-0.5d0)
    sum=sum+f(x)
  enddo
!$OMP END PARALLEL DO
  pi=w*sum
  --- TIMING BLOCK C ---
end
```



pio.f – parallelization with ordered clause

```
program compute_pi
  implicit none
  integer n,i
  double precision w,x,sum,myf,pi,f,a
  parameter (n=10 000 000)
  --- TIMING BLOCK A ---
! function to integrate
  f(a)=4.d0/(1.d0+a*a)
  --- PRINT NUM_THREADS
  --- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
  w=1.0d0/n
  sum=0.0d0
!$OMP PARALLEL PRIVATE(x,myf) , SHARED(w, sum)
!$OMP DO ORDERED
  do i=1,n
    x=w*(i-0.5d0)
    myf=f(x)
!$OMP ORDERED
      sum=sum+myf
!$OMP END ORDERED
  enddo
!$OMP END DO
!$OMP END PARALLEL
  pi=w*sum
  --- TIMING BLOCK C ---
end
```

CAUTION
The sequentialization of the ordered region may cause heavy synchronization overhead



pio2.f – ordered, but only if number of threads is fixed

```
...
!--unused-- include 'omp_lib.h'
!$ integer omp_get_num_threads
double precision w,x,sum,sum0,pi,f,a
...
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0d0/n
sum=0.0d0
!$OMP PARALLEL PRIVATE(x,sum0,num_threads), SHARED(w,sum)
sum0=0.0d0
num_threads=1
!$ num_threads=omp_get_num_threads()
!$OMP DO SCHEDULE(STATIC,(n-1)/num_threads+1)
do i=1,n
x=w*(i-0.5d0)
sum0=sum0+f(x)
enddo
!$OMP END DO
!$OMP DO ORDERED SCHEDULE(STATIC,1)
do i=1,num_threads
!$OMP ORDERED
sum=sum+sum0
!$OMP END ORDERED
enddo
!$OMP END DO
!$OMP END PARALLEL
pi=w*sum
...
```

CAUTION

1. Only if the number of threads is fixed AND if the floating point rounding is the same, then the result is the same on two different platforms and any repetition of this program.
2. This program cannot be verified with Assure because it has to call `omp_get_num_threads()`.
3. To use Assure, the second loop must be substituted by the critical region as shown in `pic2.f`

Example pi, written in Fortran (free form)

- pi.f90 – sequential code
- pi0.f90 – sequential code with a parallel region, verifying a team of threads
- pic2.f90 – parallel version with a critical region outside of the loop
- pir.f90 – parallel version with a reduction clause
- pir2.f90 – parallel version with combined `parallel for`
- pio.f90 – parallel version with ordered region
- pio2.f90 – parallel version with ordered execution if the number of threads is fixed



pi.f90 – sequential code

The timing blocks are removed on the next slides

```
program compute_pi
implicit none
! times using cpu_time
real t0,t1
!--unused-- use omp_lib
!$ double precision omp_get_wtime
!$ double precision wt0,wt1
```

timing block A.f

```
integer i
integer, parameter      :: n=10000000
real(kind=8) w,x,sum,pi,f,a
! function to integrate
f(a)=4.0_8/(1.0_8+a*a)
```

```
!$ wt0=omp_get_wtime()
call cpu_time(t0)
```

timing block B.f

```
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0_8/n
sum=0.0_8
do i=1,n
  x=w*(i-0.5_8)
  sum=sum+f(x)
enddo
pi=w*sum
```

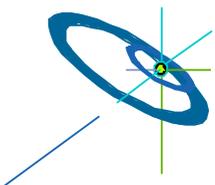
the calculation

```
call cpu_time(t1)
!$ wt1=omp_get_wtime()
write (*,'(/,a,1pg24.16)') 'computed pi = ', pi
write (*,'(/,a,1pg12.4)') 'cpu_time: ', t1-t0
!$ write (*,'(/,a,1pg12.4)') 'omp get wtime:', wt1-wt0
end program compute_pi
```

timing block C.f

pi0.f90 – only verification of team of threads – without parallelization

```
program compute_pi
implicit none
--- TIMING BLOCK A ---
integer i
integer, parameter      :: n=10000000
real(kind=8) w,x,sum,pi,f,a
!$ integer omp_get_thread_num, omp_get_num_threads
!$ integer myrank, num_threads
   logical openmp_is_used
! function to integrate
f(a)=4.0_8/(1.0_8+a*a)
!$omp parallel private(myrank, num_threads)
!$ myrank = omp_get_thread_num()
!$ num_threads = omp_get_num_threads()
!$ write (*,*) 'I am thread',myrank,'of',num_threads,'threads'
!$omp end parallel
   openmp_is_used = .false.
!$ openmp_is_used = .true.
   if (.not. openmp_is_used) then
       write (*,*) 'This program is not compiled with OpenMP'
   endif
--- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0_8/n
sum=0.0_8
do i=1,n
    x=w*(i-0.5_8)
    sum=sum+f(x)
enddo
pi=w*sum
--- TIMING BLOCK C ---
end program compute_pi
```



pic2.f90

parallelization with critical region outside of the loop

```
program compute_pi
implicit none
--- TIMING BLOCK A ---
integer i
integer, parameter :: n=10000000
real(kind=8) w,x,sum,sum0,pi,f,a
! function to integrate
f(a)=4.0_8/(1.0_8+a*a)
--- PRINT NUM_THREADS ---
--- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0_8/n
sum=0.0_8
!$OMP PARALLEL PRIVATE(x, sum0), SHARED(w, sum)
sum0=0.0_8
!$OMP DO
do i=1,n
  x=w*(i-0.5_8)
  sum0=sum0+f(x)
enddo
!$OMP END DO
!$OMP CRITICAL
  sum=sum+sum0
!$OMP END CRITICAL
!$OMP END PARALLEL
pi=w*sum
--- TIMING BLOCK C ---
end program compute_pi
```

```
!$ integer omp_get_num_threads
!$omp parallel
!$omp single
!$ write (*,*) 'OpenMP-parallel with', &
!$      omp_get_num_threads(), 'threads'
!$omp end single
!$omp end parallel
```

← shortened according to advanced practical 2

pir.f90 – parallelization with reduction clause

```
program compute_pi
implicit none
--- TIMING BLOCK A ---
integer i
integer, parameter :: n=10000000
real(kind=8) w,x,sum,pi,f,a
! function to integrate
f(a)=4.0_8/(1.0_8+a*a)
--- PRINT NUM_THREADS ---
--- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0_8/n
sum=0.0_8
!$OMP PARALLEL PRIVATE(x), SHARED(w, sum)
!$OMP DO REDUCTION(+:sum)
do i=1,n
    x=w*(i-0.5_8)
    sum=sum+f(x)
enddo
!$OMP END DO
!$OMP END PARALLEL
pi=w*sum
--- TIMING BLOCK C ---
end program compute_pi
```



pir2.f90 – combined parallel do with reduction clause

```
program compute_pi
implicit none
--- TIMING BLOCK A ---
integer i
integer, parameter :: n=10000000
real(kind=8) w,x,sum,pi,f,a
! function to integrate
f(a)=4.0_8/(1.0_8+a*a)
--- PRINT NUM_THREADS ---
--- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0_8/n
sum=0.0_8
!$OMP PARALLEL DO PRIVATE(x), SHARED(w, sum), REDUCTION(+:sum)
do i=1,n
  x=w*(i-0.5_8)
  sum=sum+f(x)
enddo
!$OMP END PARALLEL DO
pi=w*sum
--- TIMING BLOCK C ---
end program compute_pi
```



pio.f90 – parallelization with ordered clause

```
program compute_pi
implicit none
--- TIMING BLOCK A ---
integer i
integer, parameter :: n=10000000
real(kind=8) w,x,sum,myf,pi,f,a
! function to integrate
f(a)=4.0_8/(1.0_8+a*a)
--- PRINT NUM_THREADS ---
--- TIMING BLOCK B ---
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0_8/n
sum=0.0_8
!$OMP PARALLEL PRIVATE(x,myf), SHARED(w,sum)
!$OMP DO ORDERED
do i=1,n
  x=w*(i-0.5_8)
  myf=f(x)
!$OMP ORDERED
  sum=sum+myf
!$OMP END ORDERED
!$OMP END DO
!$OMP END PARALLEL
pi=w*sum
--- TIMING BLOCK C ---
end program compute_pi
```

CAUTION
The sequentialization of the ordered region may cause heavy synchronization overhead

pio2.f90 – ordered, but only if number of threads is fixed

```
...
!--unused-- use omp_lib
!$ integer omp_get_num_threads
real(kind=8) w,x,sum,sum0,pi,f,a
...
! calculate pi = integral [0..1] 4/(1+x**2) dx
w=1.0_8/n
sum=0.0_8
!$OMP PARALLEL PRIVATE(x,sum0,num_threads), SHARED(w,sum)
sum0=0.0_8
num_threads=1
!$ num_threads=omp_get_num_threads()
!$OMP DO SCHEDULE(STATIC,(n-1)/num_threads+1)
do i=1,n
  x=w*(i-0.5_8)
  sum0=sum0+f(x)
enddo
!$OMP END DO
!$OMP DO ORDERED SCHEDULE(STATIC,1)
do i=1,num_threads
!$OMP ORDERED
  sum=sum+sum0
!$OMP END ORDERED
enddo
!$OMP END DO
!$OMP END PARALLEL
pi=w*sum
...
```

CAUTION

1. Only if the number of threads is fixed AND if the floating point rounding is the same, then the result is the same on two different platforms and any repetition of this program.
2. This program cannot be verified with Assure because it has to call `omp_get_num_threads()`.
3. To use Assure, the second loop must be substituted by the critical region as shown in `pic2.f90`

heatc2.c – Parallelization of main loop and critical region (page 1 of 4) – declarations

```
#include <stdio.h>
#include <sys/time.h>
#ifdef _OPENMP
# include <omp.h>
#endif
#define min(A,B) ((A) < (B) ? (A) : (B))
#define max(A,B) ((A) > (B) ? (A) : (B))
#define imax 20
#define kmax 11
#define itmax 20000
void heatpr(double phi[imax+1][kmax+1]);

int main()
{
    double eps = 1.0e-08;
    double phi[imax+1][kmax+1], phin[imax][kmax];
    double dx,dy,dx2,dy2,dx2i,dy2i,dt,dphi,dphimax,dphimax0;
    int i,k,it;
    struct timeval tv1,tv2; struct timezone tz;
# ifdef _OPENMP
    double wt1,wt2;
# endif

# ifdef _OPENMP
# pragma omp parallel
    {
        pragma omp single
        printf("OpenMP-parallel with %1d threads\n",
            omp_get_num_threads());
    } /* end omp parallel */
# endif
}
```



H L R I S 

heatc2.c (page 2 of 4) – initialization

```
    dx=1.0/kmax;   dy=1.0/imax;
    dx2=dx*dx;    dy2=dy*dy;
    dx2i=1.0/dx2; dy2i=1.0/dy2;
    dt=min(dx2,dy2)/4.0;
/* start values 0.d0 */
#pragma omp parallel private(i,k) shared(phi)
{
#pragma omp for
  for (k=0;k<kmax;k++)
  { for (i=1;i<imax;i++)
    { phi[i][k]=0.0;
      }
    }
/* start values 1.d0 */
#pragma omp for
  for (i=0;i<=imax;i++)
  { phi[i][kmax]=1.0;
    }
}/*end omp parallel*/
/* start values dx */
phi[0][0]=0.0;
phi[imax][0]=0.0;
for (k=1;k<kmax;k++)
{ phi[0][k]=phi[0][k-1]+dx;
  phi[imax][k]=phi[imax][k-1]+dx;
}
printf("\nHeat Conduction 2d\n");
printf("\ndx = %12.4g, dy = %12.4g, dt = %12.4g, eps = %12.4g\n",
       dx,dy,dt,eps);
printf("\nstart values\n");
heatpr(phi);
```



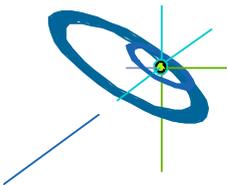
H L R I S 

heatc2.c (page 3 of 4) – time step integration

```
gettimeofday(&tv1, &tz);
# ifdef _OPENMP
    wt1=omp_get_wtime();
# endif
/* iteration */
for (it=1;it<=itmax;it++)
{ dphimax=0.;
#pragma omp parallel private(i,k,dphi,dphimax0) \
    shared(phi,phin,dx2i,dy2i,dt,dphimax)
{
    dphimax0=dphimax;
#pragma omp for
    for (k=1;k<kmax;k++)
    { for (i=1;i<imax;i++)
        { dphi=(phi[i+1][k]+phi[i-1][k]-2.*phi[i][k])*dy2i
            +(phi[i][k+1]+phi[i][k-1]-2.*phi[i][k])*dx2i;
          dphi=dphi*dt;
          dphimax0=max(dphimax0,dphi);
          phin[i][k]=phi[i][k]+dphi;
        }
    }
#pragma omp critical
{    dphimax=max(dphimax,dphimax0);
}
/* save values */
#pragma omp for
    for (k=1;k<kmax;k++)
    { for (i=1;i<imax;i++)
        { phi[i][k]=phin[i][k];
        }
    }
}/*end omp parallel*/
    if(dphimax<eps) break;
}
```

Caution:

In C, phi and phin are contiguous in the last index [k]. Therefore the k-loop should be the inner loop!



H L R I S 

heatc2.c (page 4 of 4) – wrap up

```
# ifdef _OPENMP
    wt2=omp_get_wtime();
# endif
gettimeofday(&tv2, &tz);
printf("\nphi after %d iterations\n",it);
heatpr(phi);
# ifdef _OPENMP
    printf( "wall clock time (omp_get_wtime) = %12.4g sec\n", wt2-wt1 );
# endif
printf( "wall clock time (gettimeofday) = %12.4g sec\n", (tv2.tv_sec-
    tv1.tv_sec) + (tv2.tv_usec-tv1.tv_usec)*1e-6 );
}

void heatpr(double phi[imax+1][kmax+1])
{ int i,k,kl,kk,kkk;
  kl=6;  kkk=kl-1;
  for (k=0;k<=kmax;k=k+kl)
  { if(k+kkk>kmax) kkk=kmax-k;
    printf("\ncolumns %5d to %5d\n",k,k+kkk);
    for (i=0;i<=imax;i++)
    { printf("%5d ",i);
      for (kk=0;kk<=kkk;kk++)
      { printf("#%12.4g",phi[i][k+kk]);
        }
      printf("\n");
    }
  }
}

return;
}
```

heatr2_x.f – Parallelization of main loop with reduction clause (page 1 of 4) – declarations

```
program heat
  implicit none
  integer i,k,it, imax,kmax,itmax
c using reduction
  parameter (imax=20,kmax=11)
  parameter (itmax=20000)
  double precision eps
  parameter (eps=1.d-08)
  double precision phi(0:imax,0:kmax), phin(1:imax-1,1:kmax-1)
  double precision dx,dy,dx2,dy2,dx2i,dy2i,dt,dphi,dphimax
! times using cpu_time
  real t0
  real t1
!---unused-- include 'omp_lib.h'
!$ integer omp_get_num_threads
!$ double precision omp_get_wtime
!$ double precision wt0,wt1
!
!$omp parallel
!$omp single
!$ write(*,*) 'OpenMP-parallel with',omp_get_num_threads(),'threads'
!$omp end single
!$omp end parallel
C
  dx=1.d0/kmax
  dy=1.d0/imax
  dx2=dx*dx
  dy2=dy*dy
  dx2i=1.d0/dx2
  dy2i=1.d0/dy2
  dt=min(dx2,dy2)/4.d0
```



H L R I S 

heatr2_x.f (page 2 of 4) – initialization

```
!$OMP PARALLEL PRIVATE(i,k), SHARED(phi)
c start values 0.d0
!$OMP DO
  do k=0,kmax-1
    do i=1,imax-1
      phi(i,k)=0.d0
    enddo
  enddo
!$OMP END DO
c start values 1.d0
!$OMP DO
  do i=0,imax
    phi(i,kmax)=1.d0
  enddo
!$OMP END DO
!$OMP END PARALLEL
c start values dx
phi(0,0)=0.d0
phi(imax,0)=0.d0
do k=1,kmax-1
phi(0,k)=phi(0,k-1)+dx
phi(imax,k)=phi(imax,k-1)+dx
enddo
c print array
write (*,'(/,a)')
f      'Heat Conduction 2d'
write (*,'(/,4(a,1pg12.4))')
f      'dx =',dx,', dy =',dy,', dt =',dt,', eps =',eps
write (*,'(/,a)')
f      'start values'
call heatpr(phi,imax,kmax)
```

H L R I S



heatr2_x.f (page 3 of 4) – time step integration

```
!$      wt0=omp_get_wtime()
      call cpu_time(t0)

c iteration
      do it=1,itmax
      dphimax=0.
!$OMP PARALLEL PRIVATE(i,k,dphi), SHARED(phi,phin,dx2i,dy2i,dt,dphimax)
!$OMP DO REDUCTION(max:dphimax)
      do k=1,kmax-1
      do i=1,imax-1
      dphi=(phi(i+1,k)+phi(i-1,k)-2.*phi(i,k))*dy2i
f          +(phi(i,k+1)+phi(i,k-1)-2.*phi(i,k))*dx2i
      dphi=dphi*dt
      dphimax=max(dphimax,dphi)
      phin(i,k)=phi(i,k)+dphi
      enddo
      enddo
!$OMP END DO
c save values
!$OMP DO
      do k=1,kmax-1
      do i=1,imax-1
      phi(i,k)=phin(i,k)
      enddo
      enddo
!$OMP END DO
!$OMP END PARALLEL
      if(dphimax.lt.eps) goto 10
      enddo
10      continue
```

In Fortran, phi and phin are contiguous in the first index [i]. Therefore the i-loop should be the inner loop!
This optimization is done in all heat..._x.f versions



heatr2_x.f (page 4 of 4) – wrap up

```
call cpu_time(t1)
!$ wt1=omp_get_wtime()

c print array
write (*, '(/,a,i6,a)')
f      'phi after',it,' iterations'
write (*, '(/,a,1pg12.4)') 'cpu_time : ', t1-t0
!$ write (*, '(/,a,1pg12.4)') 'omp_get_wtime:', wt1-wt0
c
c      stop
c      end

c
c
c      subroutine heatpr(phi,imax,kmax)
c      double precision phi(0:imax,0:kmax)
c
c      kl=6
c      kkk=kl-1
c      do k=0,kmax,kl
c      if(k+kkk.gt.kmax) kkk=kmax-k
c      write (*, '(/,a,i5,a,i5)') 'columns',k,' to',k+kkk
c      do i=0,imax
c      write (*, '(i5,6(1pg12.4))') i, (phi(i,k+kk),kk=0,kkk)
c      enddo
c      enddo

c
c      return
c      end
```

False-sharing – an experiment (solution/pi/piarr.c)

```
n = 100000000;    w=1.0/n;    sum=0.0;
stride=1;  if (argc>1) stride=atoi(argv[1]);  /* unit is "double" */

#pragma omp parallel private (x,index) shared(w,sum,p_sum)
{
  # ifdef _OPENMP
    index=stride*omp_get_thread_num();
  # else
    index=0;
  # endif
  p_sum[index]=0;
  #pragma omp for
  for (i=1;i<=n;i++)
  {
    x=w*((double)i-0.5);
    p_sum[index+(x>1?1:0)] = p_sum[index] + 4.0/(1.0+x*x);
    /* The term (x>1?1:0) is always zero. It is used to prohibit
       register caching of of p_sum[index], i.e., to guarantee that
       each access to this variable is done via cache in the memory. */
  }
  #pragma omp critical
  {
    sum=sum+p_sum[index];
  }
}
pi=w*sum;
```

The thread-locality of psum[index] variables is forced manually, and in the same cache-line if stride is small enough



